



# *Presentation of MSc's Thesis*



## **'A Framework for Building Transient Well Testing Numerical Models Using Unstructured Grids'**

By:

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**Title of Thesis:**

A Framework for Rapid Numerical Well Test Analysis Using an Open Source Simulator

**Key Words:**

Well Testing; Simulation; Unstructured Grids; MRST; Eclipse

**Summary:**

In conjunction with the Open Porous Media (OPM), SINTEF Company in Oslo have released the Matlab Reservoir Simulation Toolbox (MRST) aiming to function as an efficient platform for implementing new ideas and discretization methods in reservoir simulations applications. MRST has been developed as an open source program under the General Public License (GPL<sup>1</sup>), and in this thesis, the author intends to modify the existing source code of MRST (Release: 2016b) to implement an unstructured gridding algorithm has the ability to conform the basic geological features of the reservoir as an extension to the black oil framework. The governing equations are evaluated using the finite-volume method and the system of equations is solved fully-implicitly using the Newton-Raphson method. The created model in this thesis is used to build a numerical well testing models to tune the analytical solution results, validated versus the recorded pressure signals from the test, the analytical type curves, and Schlumberger reservoir simulator; Eclipse, to give a better representation for the geological features and the petro-physical properties of the reservoir using an easy procedure to construct the grid and to assign these properties.

<sup>1</sup> <http://www.gnu.org/licenses/gpl.html>

# Application Cases: Numerical Well Testing

## Pressure Transient Testing

**John Lee**

Peterson Chair and Professor of Petroleum Engineering  
Texas A&M.U.

**John B. Rollins**

Senior Technical Consultant  
International Business Machines Corp.

**John P. Spivey**

Principal Reservoir Engineer  
Schlumberger

**\*\*2003**

To validate versus the pressure signals and Eclipse, we used:

Normalized Root Mean Square Error (NRMSE)

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^n (X_{\text{obs},i} - X_{\text{model},i})^2}{n}}$$

$$\text{NRMSE} = \frac{\text{RMSE}}{X_{\text{obs,max}} - X_{\text{obs,min}}}$$

To do sensitivities over the analytical solution parameters, we used:

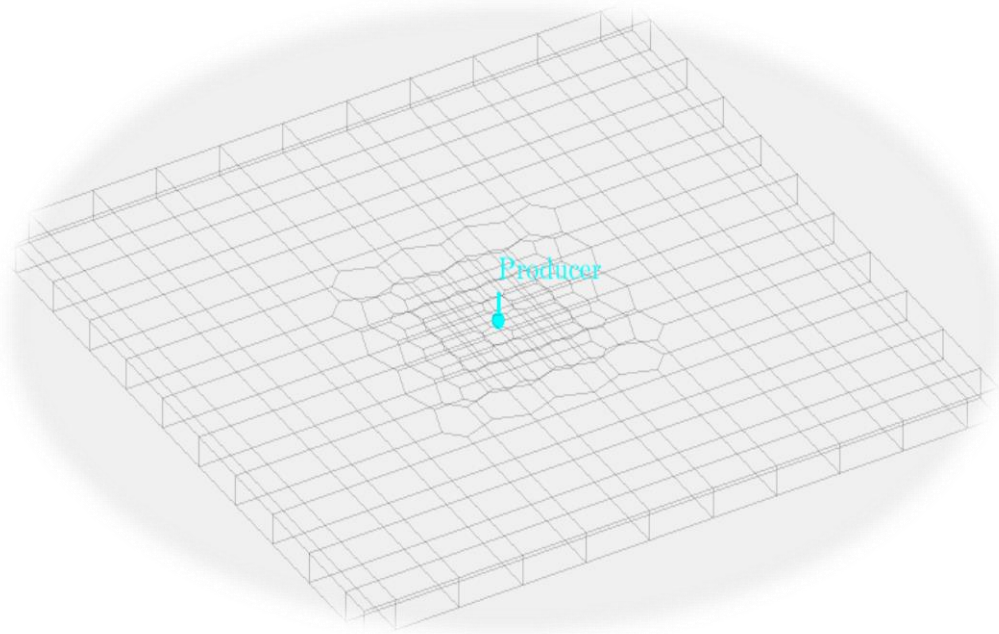
Mean Absolute Relative Error (MARE)

$$\text{MARE} = \frac{100}{n} \sum_{i=1}^n |O_i - P_i| / |O_i|$$

# Hybrid Grid, Single Well, 7 Cases Compared to Eclipse Cartesian Grid

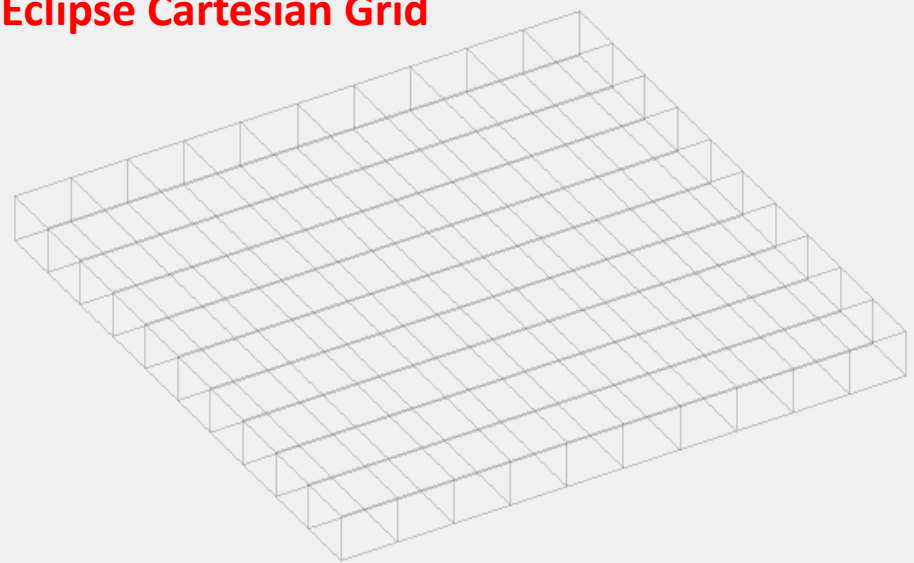
# of Grids 193, 1 to 3 Newton Iter./T.S., CPU Time=4 Secs

Case	Test Type	Phase
1	Draw Down	Oil
2	Variable Rate Draw Down	Oil
3	Build Up	Oil
4	Build Up After Variable Rate Draw Down	Oil
5	Build Up	Gas
6	Injectivity	Water
7	Fall Off	Water



## Indexing

### Eclipse Cartesian Grid

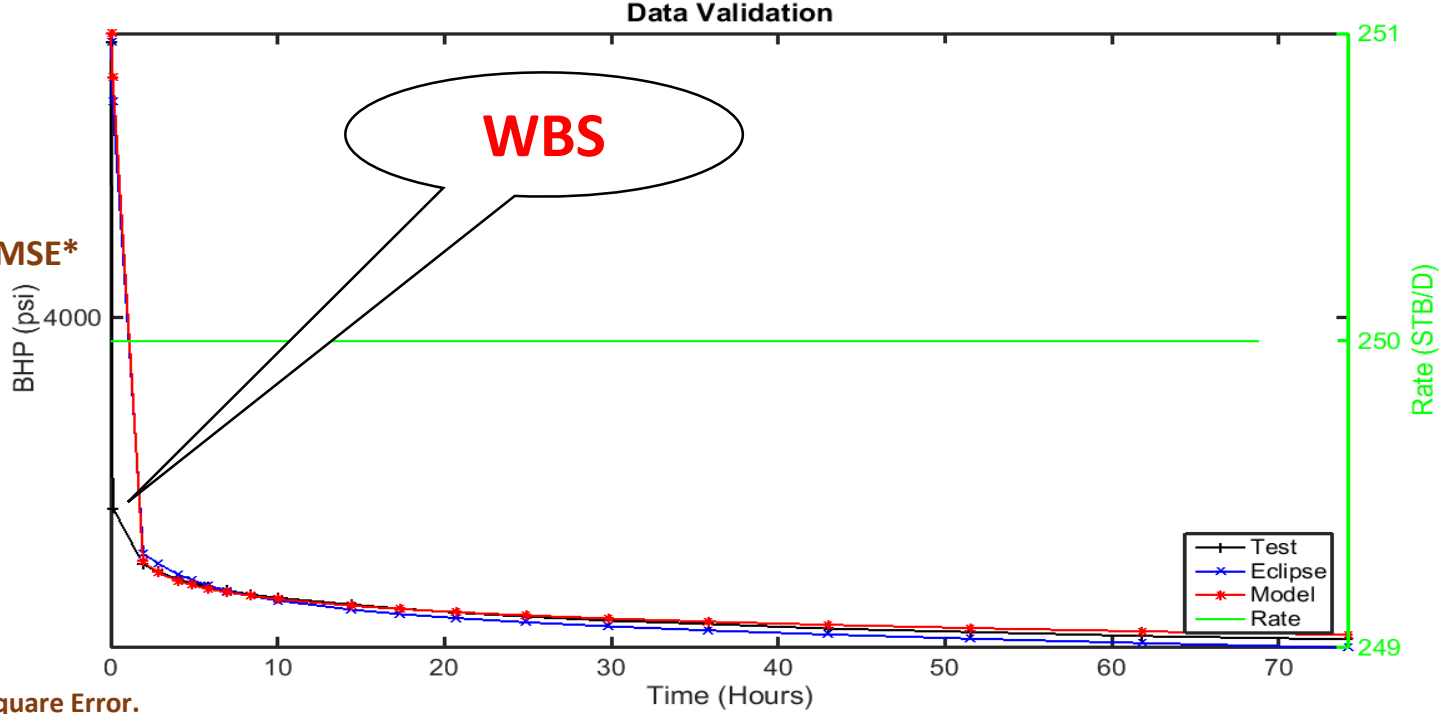


193	192	191	190	189	188	187	186	185	184	183										
182	181	180	179	178	177	176	175	174	173	172										
171	170	169	168	167	166	165	164	163	162	161										
160	159	158	157	156	155	154	153	152	151	150										
149	148	147	146	139	140	129	130	122	123	121										
				145	141	142	135	134	133	125	126									
				104	144	143	138	137	134	133	281	27								
				104	105	106	92	93	95	96	82	83								
				104	108	107	94	97	98	84	86									
				117	117	116	115	114	109	101	1	98	88	89	87	81	80	79	78	
				77	76	75	74	113	112	111	103	102	99	91	90	54	49	48	47	46
				77	76	75	74	67	68	69	57	58	61	62	50	51				
				77	76	75	74	73	71	70	60	59	64	63	53	52				
				45	44	43	42	73	72	66	65	66	65	56	55					
				45	44	43	42	41	40	39	38	37	36	35						
				34	33	32	31	30	29	28	27	26	25	24						
				23	22	21	20	19	18	17	16	15	14	13						
				12	11	10	9	8	7	6	5	4	6	3	2					

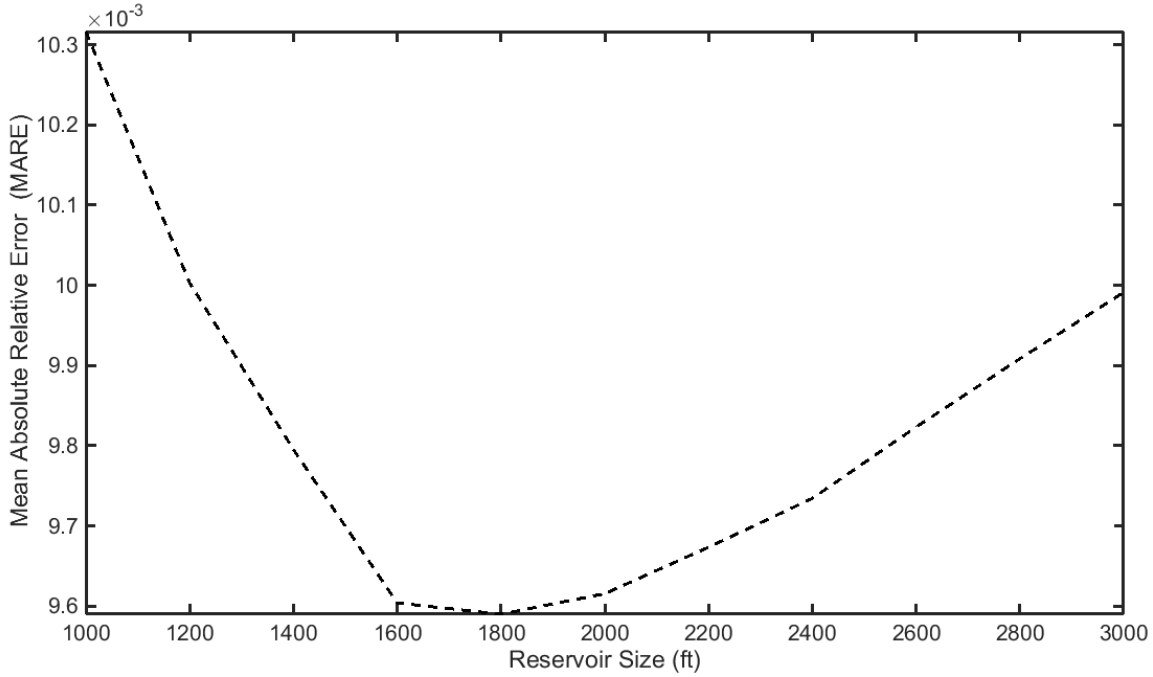
Case_ Source	Test Type	Phase	Givens (Model Parameters)
1_ Ex:2.1	Draw Down	Oil	$Q_o = 250$ STB/D, $h = 69$ ft, $\phi = 0.039$ , $B_o = 1.136$ RB/STB, $P_i = 4,412$ psia, $C_t = 17 \times 10^{-6}$ psi <sup>-1</sup> , $r_w = 0.198$ ft, and $\mu = 0.8$ cp
2_ Ex:2.3	A 3-hour Variable Rate Draw Down	Oil	1 <sup>st</sup> hour averaged 478.5 STB/D; 2 <sup>nd</sup> hour, 319 STB/D; and 3 <sup>rd</sup> hour, 159.5 STB/D, $h = 10$ ft, $\phi = 0.12$ , $B_o = 1.2$ RB/STB, $P_i = 3,000$ psia, $C_t = 48 \times 10^{-6}$ psi <sup>-1</sup> , $r_w = 0.25$ ft, and $\mu = 0.6$ cp
3_ Ex:2.4	Build Up	Oil	after constant rate of 500 STB/D for 3 days $h = 22$ ft, $\phi = 0.2$ , $B_o = 1.3$ RB/STB, $P_{wf} = 1,150$ psia, $C_t = 20 \times 10^{-6}$ psi <sup>-1</sup> , $r_w = 0.3$ ft, and $\mu = 1$ cp
4_ Ex:2.6	Build Up After Variable Rate Draw Down	Oil	Time Interval      Production Rate (hours)                      (STB/D) 0 to 3                      398.8 3 to 6                      265.8 6 to 9                      132.9 $h = 22$ ft, $\phi = 0.12$ , $B_o = 1.2$ RB/STB, $C_t = 4.8 \times 10^{-5}$ psi <sup>-1</sup> , $r_w = 0.25$ ft, and $\mu = 0.6$ cp
5_ Ex:3.3	Build Up	Gas	$\gamma_g = 0.7$ , $Q_g = 5,256$ Mscf/D, $t_p = 2000$ hrs, $z = 0.8678$ , $T = 640^\circ\text{R}$ ( $180^\circ\text{F}$ ), $h = 28$ ft, $\phi = 0.18$ , $B_g = 0.962$ RB/ Mscf, $P_i = 2,906$ psia, $C_t = 2.238 \times 10^{-4}$ psi <sup>-1</sup> , $r_w = 0.3$ ft, and $\mu = 0.01885$ cp
6_ Ex:9.1	Injectivity	Water	$Q_w = -100$ STB/D, $h = 16$ ft, $\phi = 0.15$ , $B_w = 1$ RB/STB, $P_i = 449$ psia, $C_t = 7.7 \times 10^{-6}$ psi <sup>-1</sup> , $r_w = 0.25$ ft, and $\mu = 1$ cp
7_ Ex:9.2	Fall Off	Water	$Q_w = -807$ STB/D, $h = 28$ ft, $\phi = 0.25$ , $B_w = 1$ RB/STB, $P_i = 2,788$ psia, $C_t = 1.18 \times 10^{-5}$ psi <sup>-1</sup> , $r_w = 0.4$ ft, and $\mu = 1$ cp

# Case\_1: DD-Oil

Goodness of Fit Based on NRMSE\*  
 Relative to Test Points:  
 1- Eclipse= **0.0101**  
 2- Model= **0.0096** ↓



NRMSE\*: Normalized Root Mean Square Error.

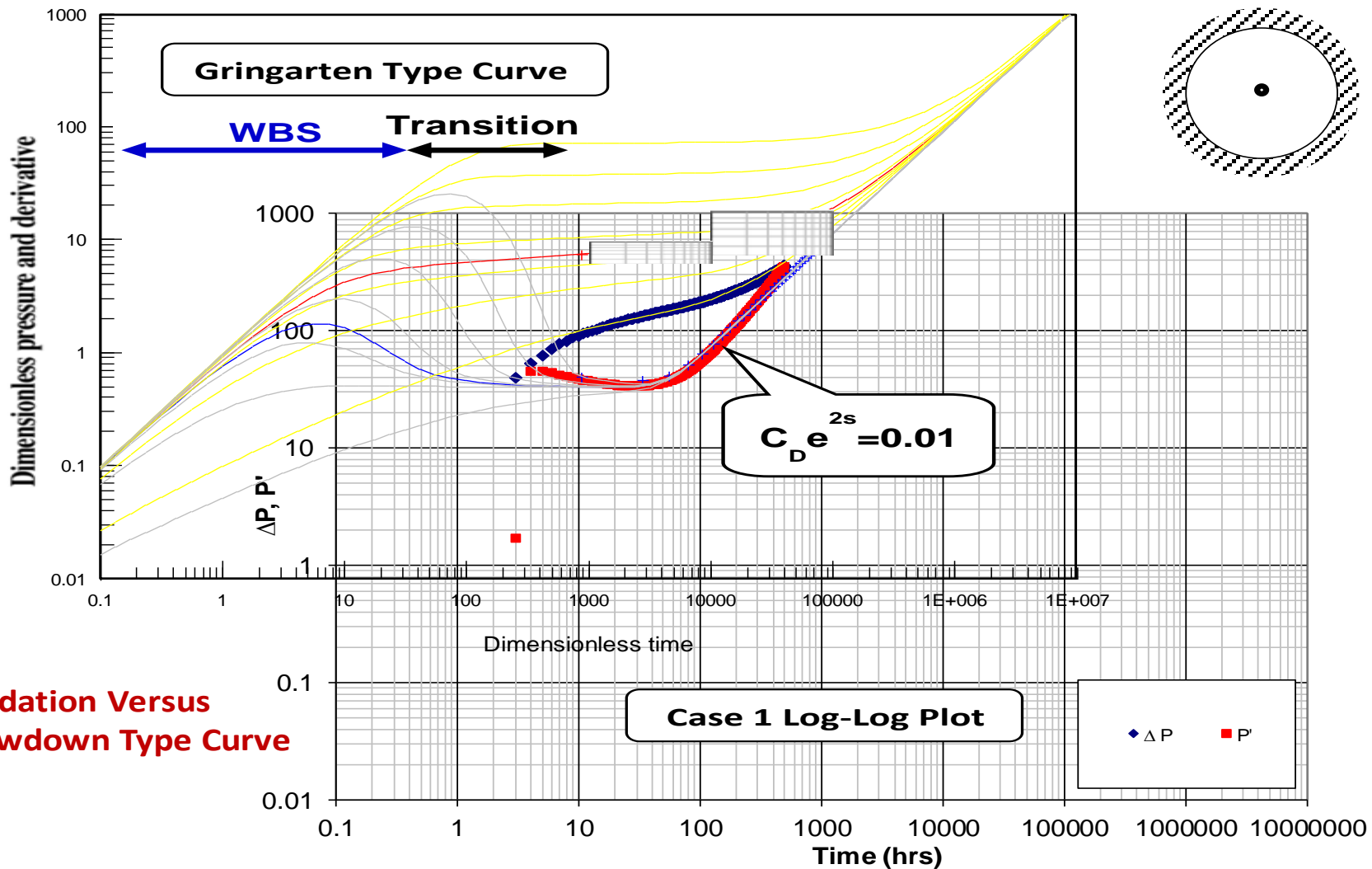


**Sensitivity over Reservoir Size to Give Minimum Error:**

- 1- Analytical Solution, **Infinite Reservoir (N/A)**
- 2- Model, **Re = 1800 ft**

# Case\_1: Validation Versus The Analytical Solution

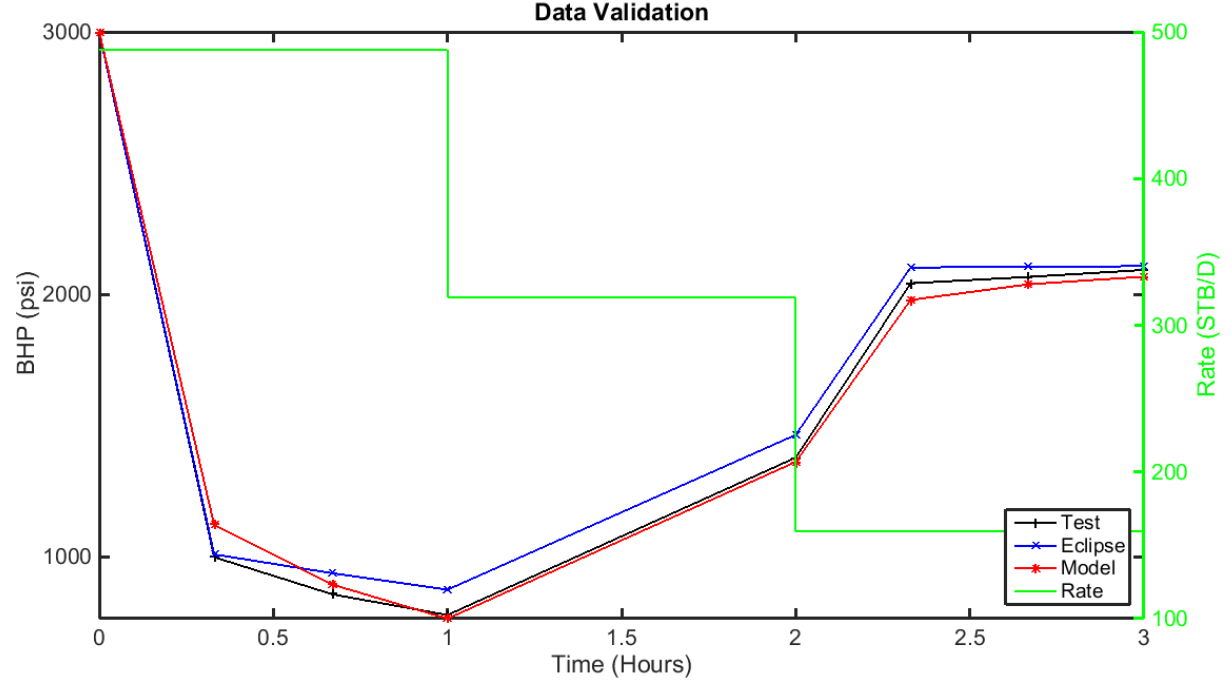
Closed Circular Boundary



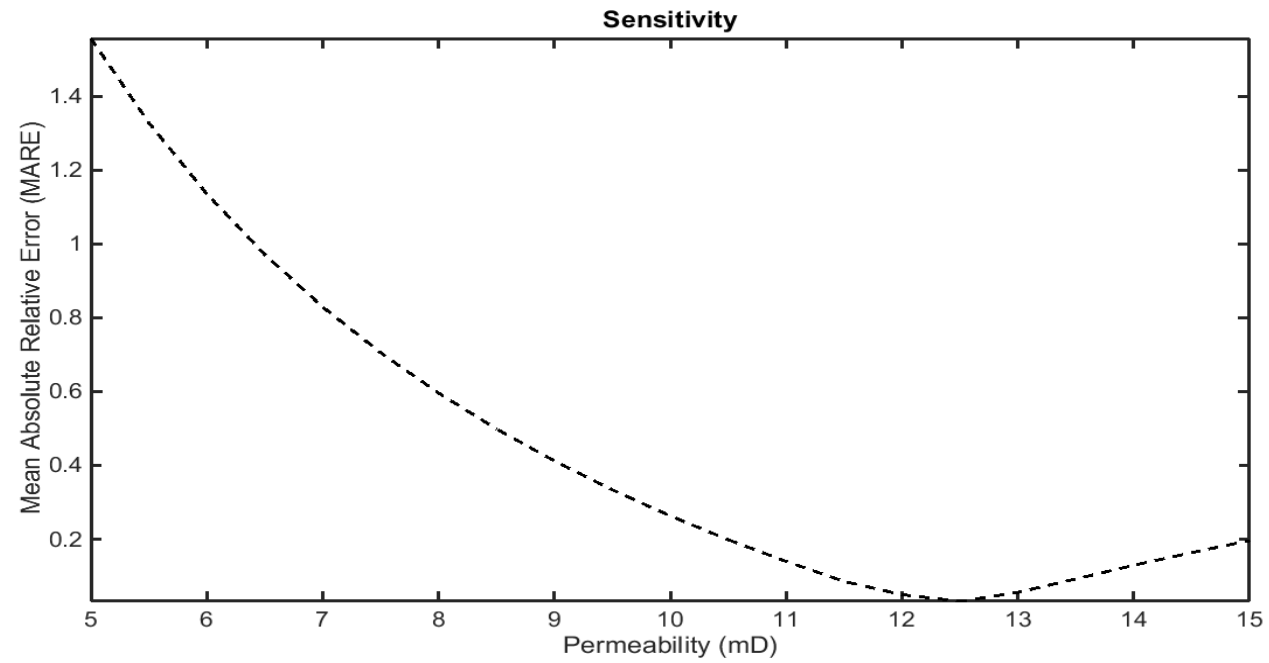
# Case\_2: Variable Rate DD-Oil

Goodness of Fit Based on NRMSE\*  
Relative to Test Points:

- 1- Eclipse= **0.044**
- 2- Model= **0.031** ↓



NRMSE\*: Normalized Root Mean Square Error.



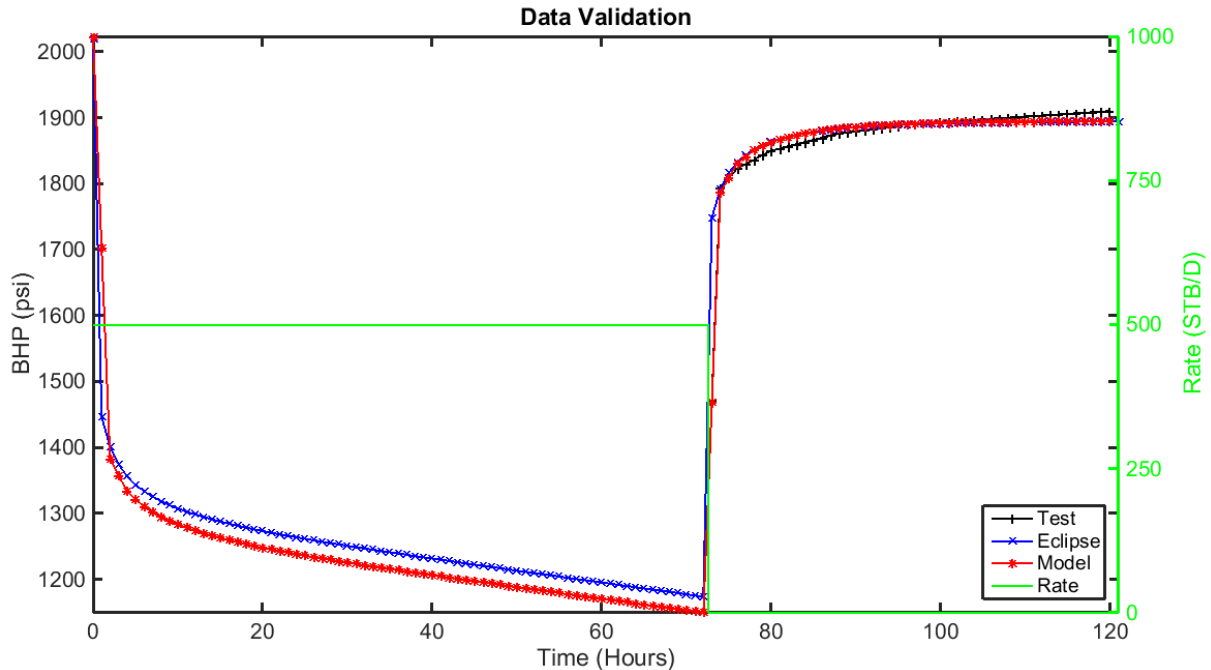
**Sensitivity over  
Reservoir Permeability  
to Give Minimum Error:**

- 1- Analytical Solution, K= **12.5 mD**
- 2- Model , K = **12.5 mD**

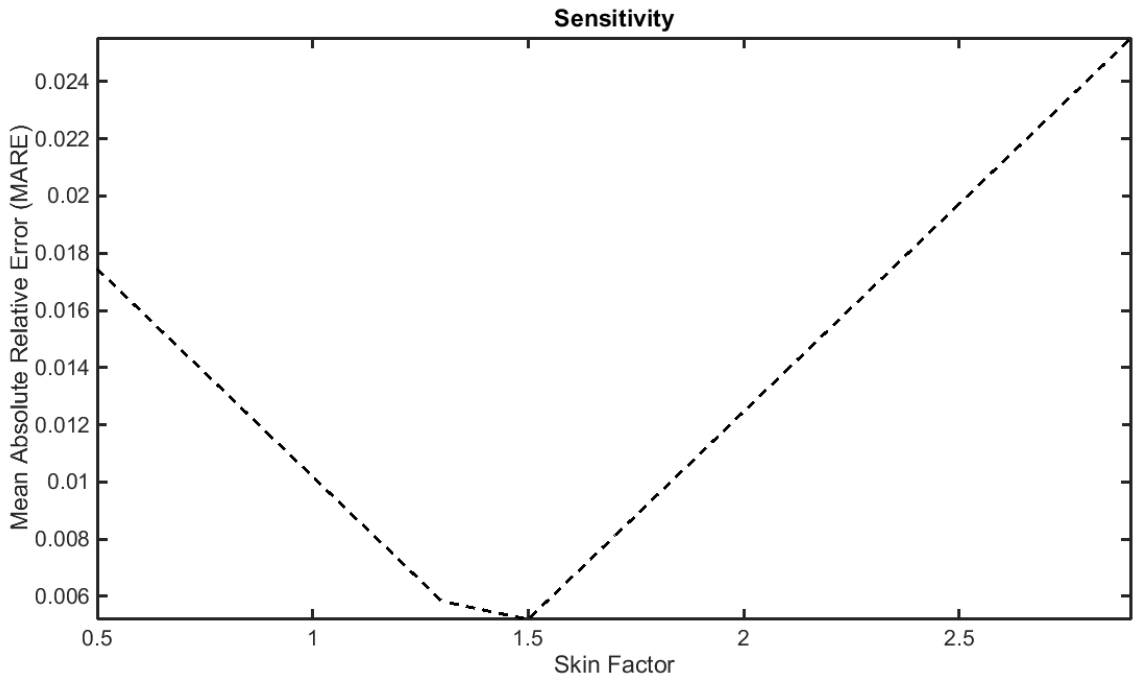


# Case\_3: BU-Oil

Goodness of Fit Based on NRMSE\*  
 Relative to Test Points:  
 1- Eclipse= **0.0067**  
 2- Model= **0.0042** ↓



NRMSE\*: Normalized Root Mean Square Error.

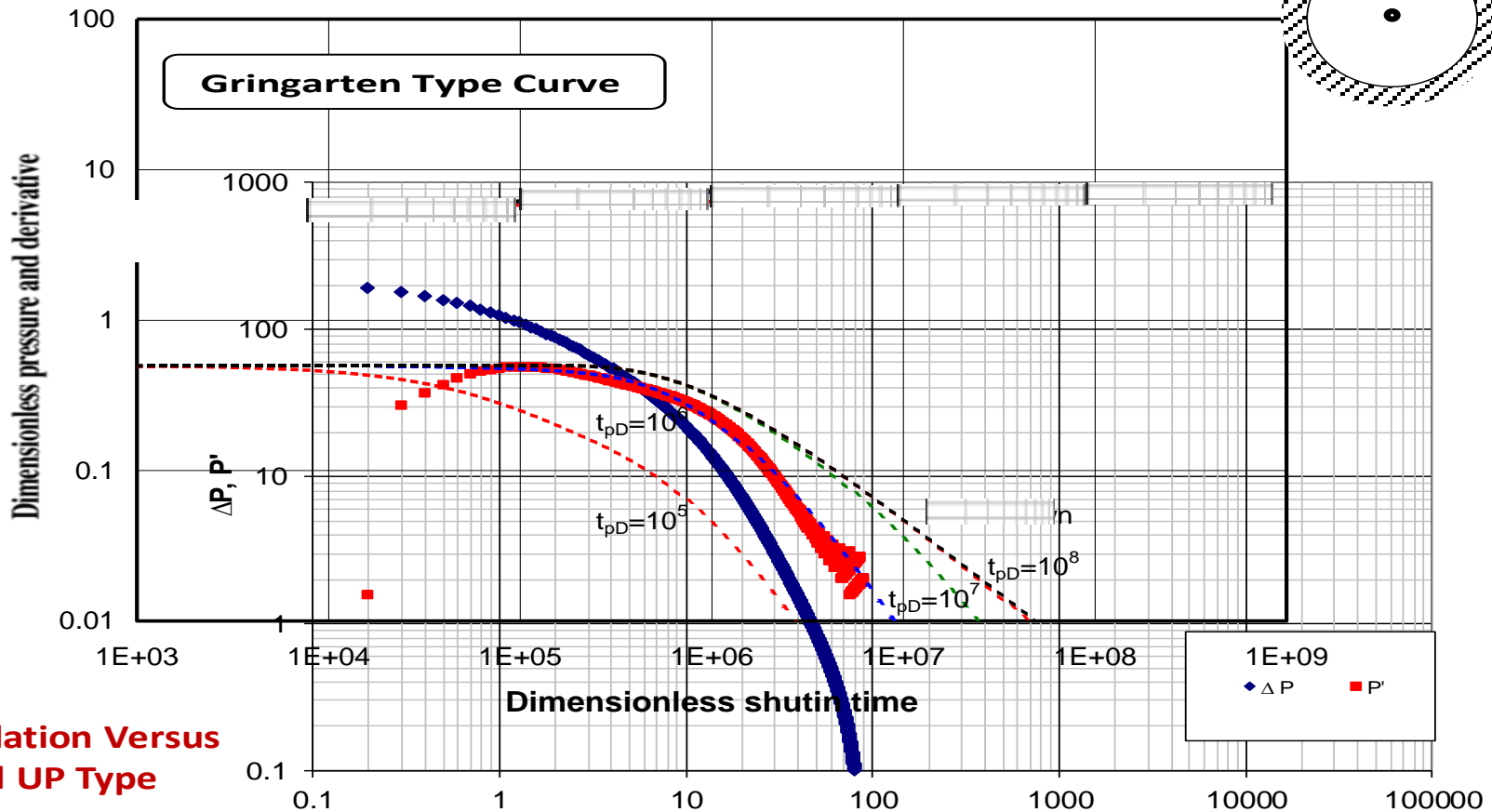
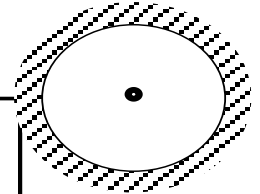


**Sensitivity over Skin Factor to Give Minimum Error:**

- 1- Analytical Solution, S= **1.43**
- 2- Model , S = **1.5**

# Case\_3: Validation Versus The Analytical Solution

Closed Circular Boundary



Validation Versus  
Build UP Type  
Curve

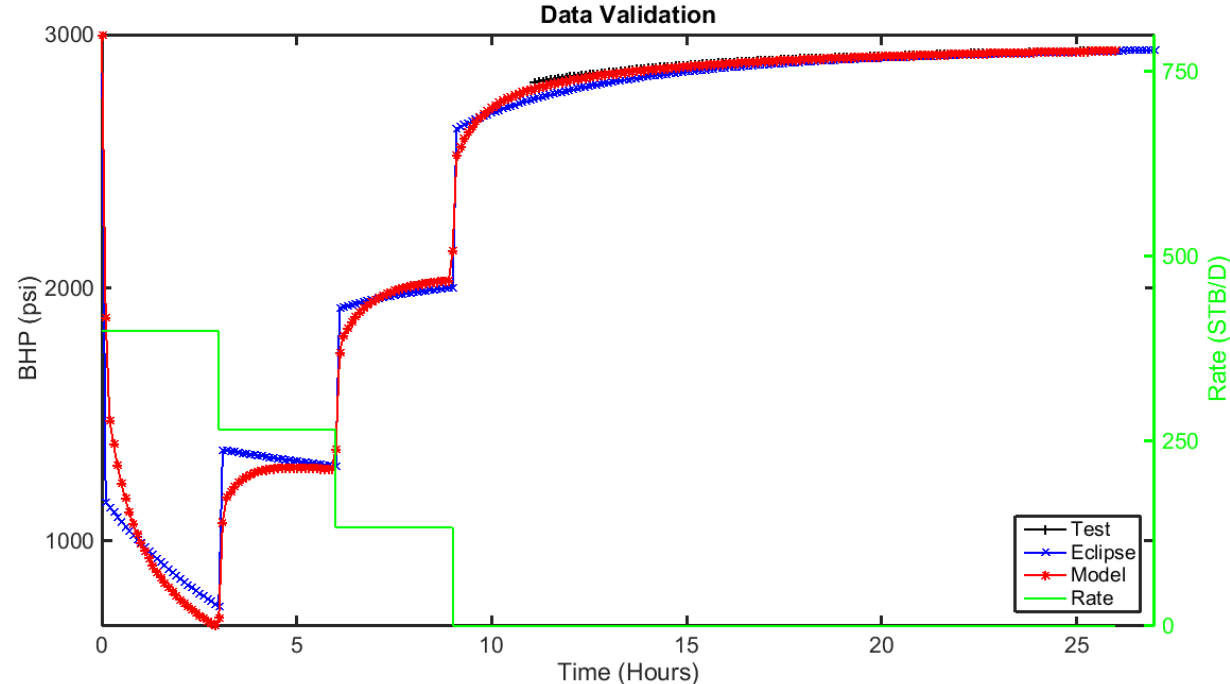
Case 3 Log-Log Plot

# Case\_4: Variable Rate BU-Oil

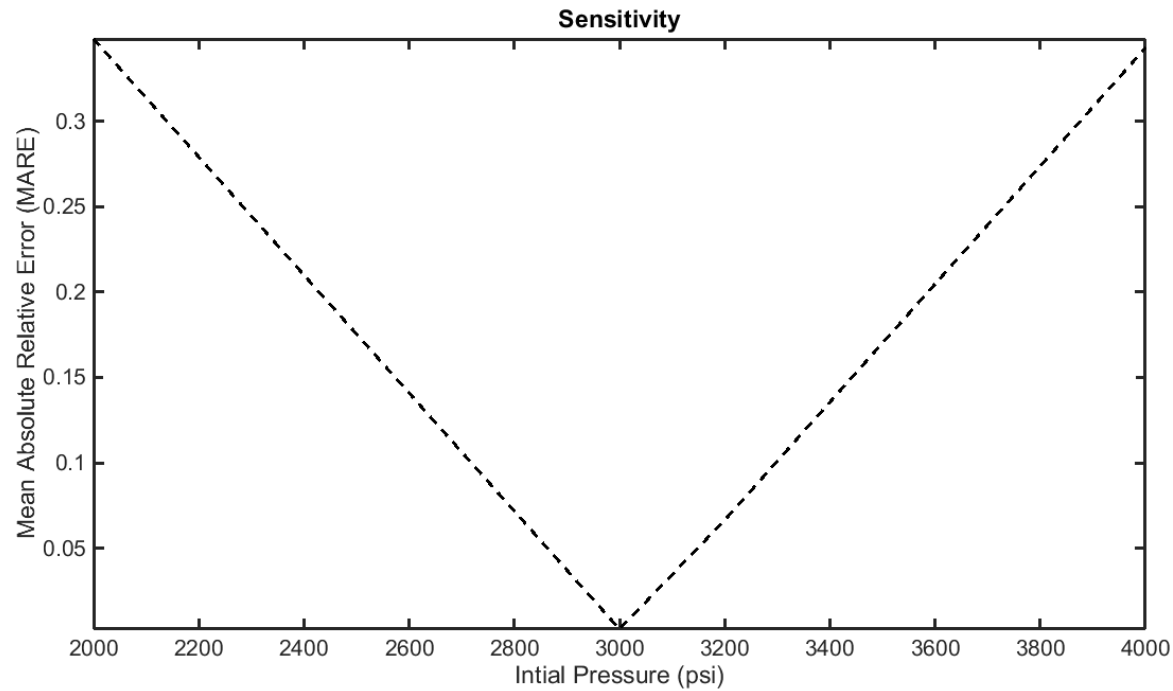
Goodness of Fit Based on NRMSE\*  
Relative to Test Points:

1- Eclipse= **0.009**

2- Model= **0.002**



NRMSE\*: Normalized Root Mean Square Error.



**Sensitivity over Initial Pressure to Give Minimum Error:**

1- Analytical Solution,  $P_i = 3000$  psi

2- Model,  $P_i = 3000$  psi

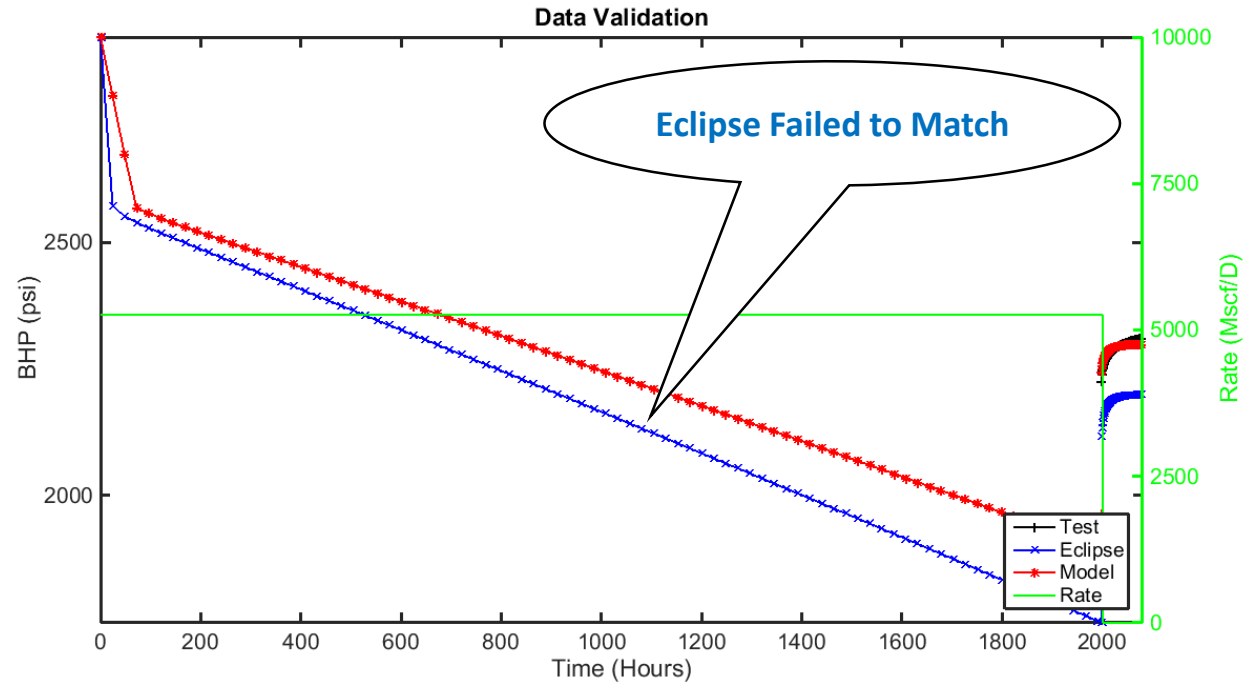
# Case\_5: BU-Gas

Goodness of Fit Based on NRMSE\*

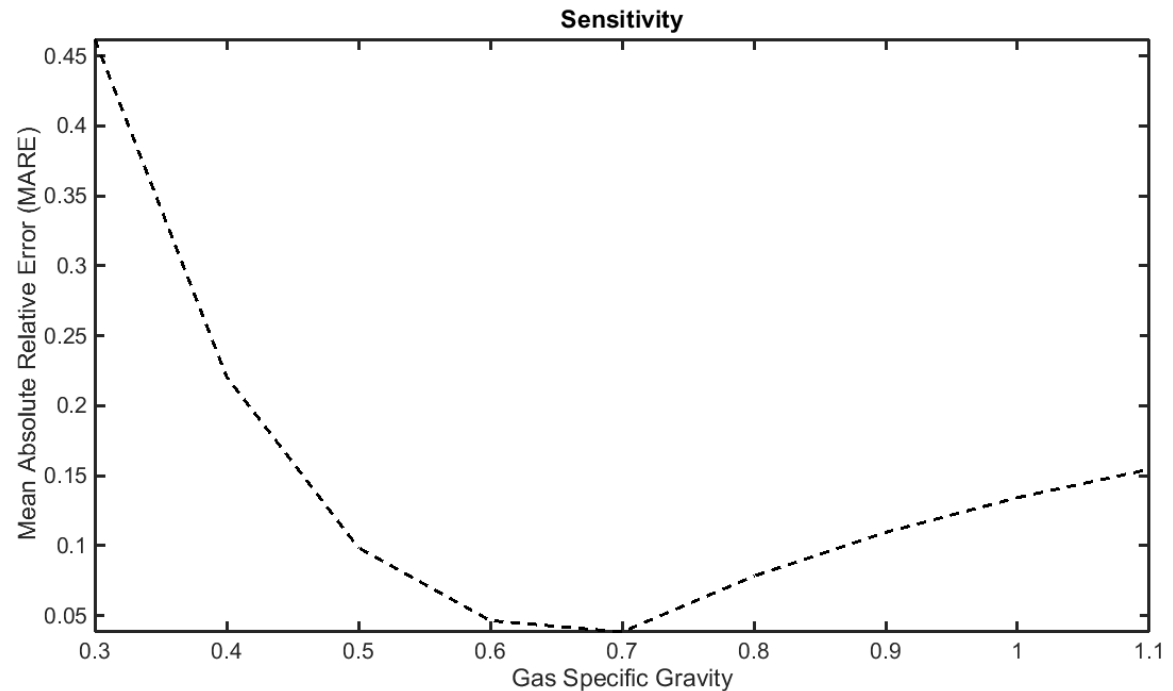
Relative to Test Points:

1- Eclipse= **0.098**

2- Model= **0.0038**



NRMSE\*: Normalized Root Mean Square Error.



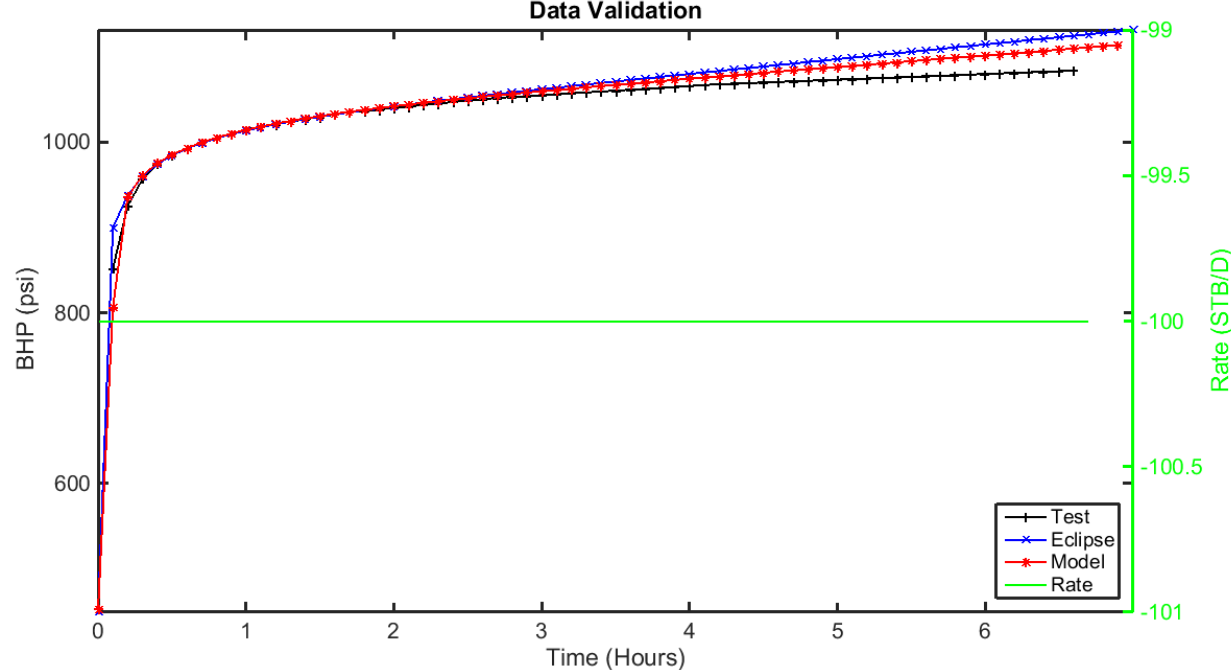
**Sensitivity over Gas Specific Gravity to Give Minimum Error:**

1- Analytical Solution,  $\gamma_g = 0.7$

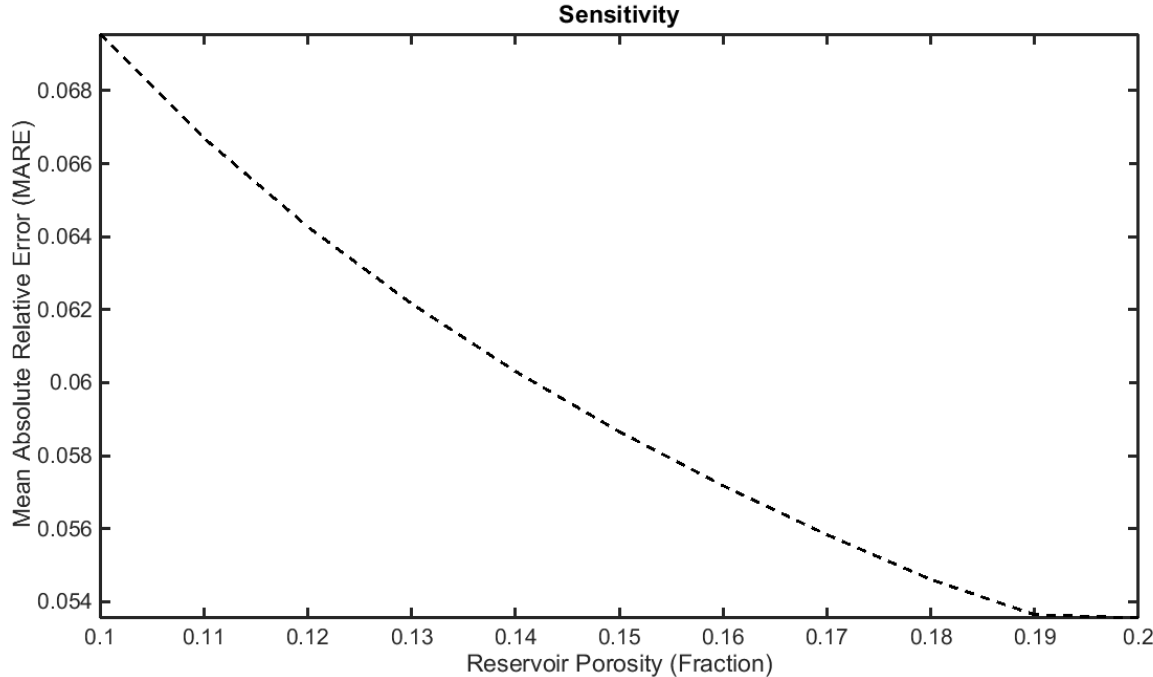
2- Model,  $\gamma_g = 0.7$

# Case\_6: Inj. Test-Water

Goodness of Fit Based on NRMSE\*  
 Relative to Test Points:  
 1- Eclipse= **0.012**  
 2- Model= **0.010** ↓



NRMSE\*: Normalized Root Mean Square Error.

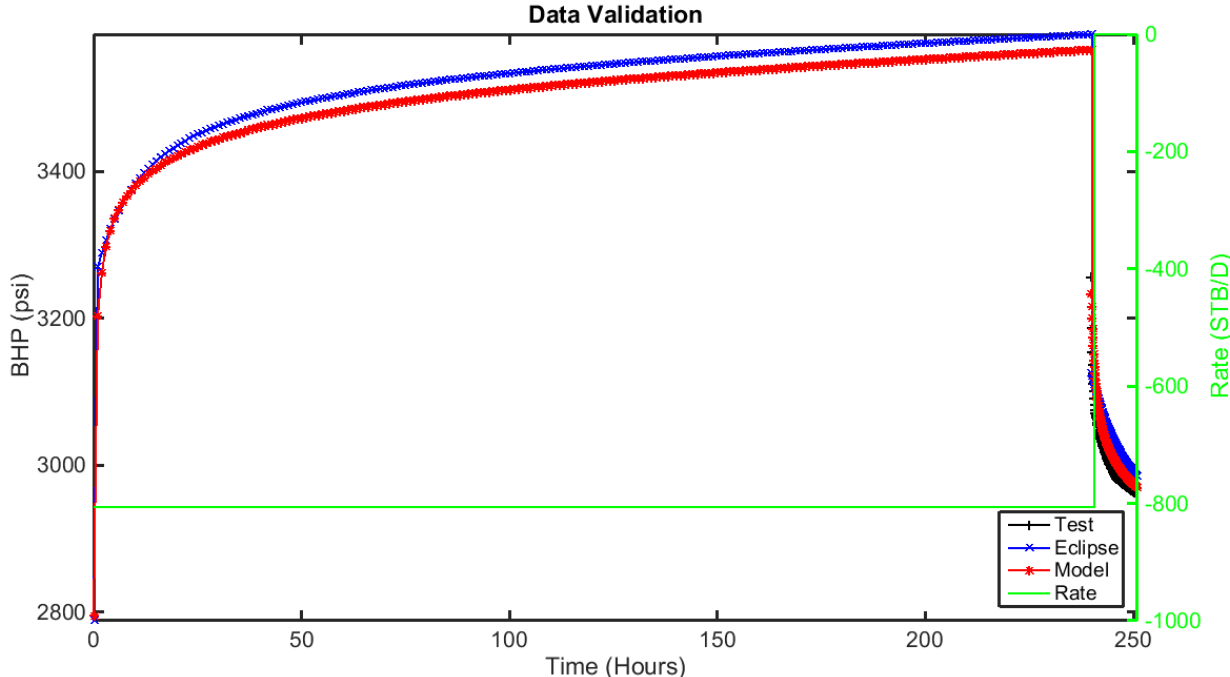


**Sensitivity over Reservoir Porosity to Give Minimum Error:**

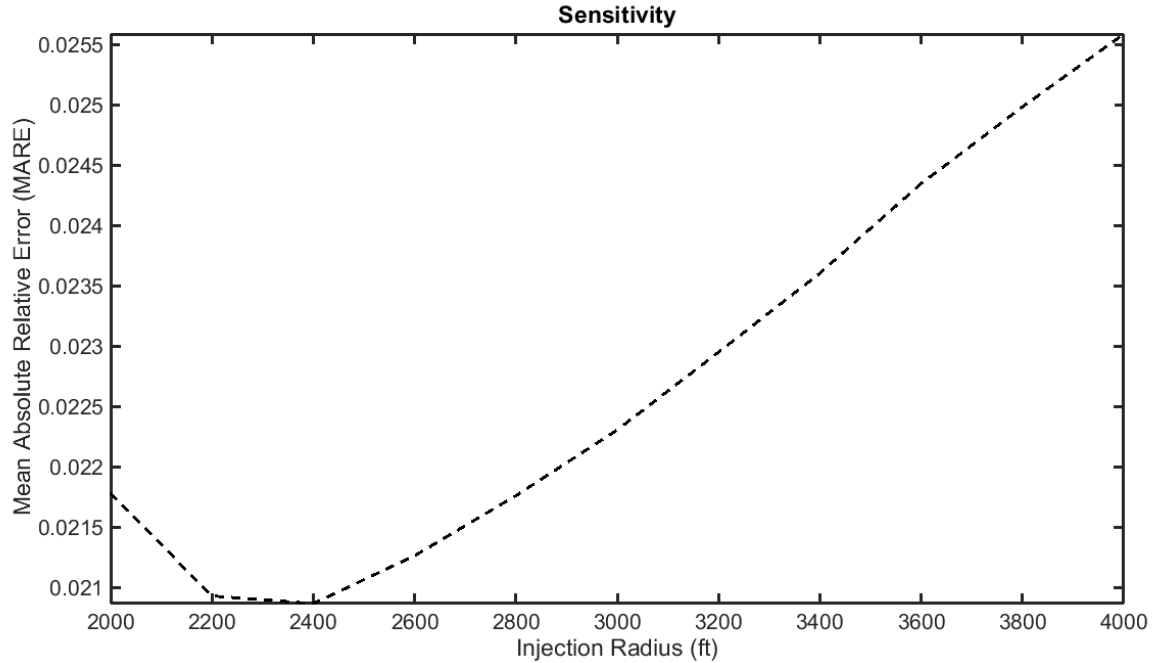
- 1- Analytical Solution,  $\phi = 0.15$
- 2- Model,  $\phi = 0.19$

# Case\_7: Fall Off Test-Water

Goodness of Fit Based on NRMSE\*  
 Relative to Test Points:  
 1- Eclipse= **0.02**  
 2- Model= **0.014** ↓



NRMSE\*: Normalized Root Mean Square Error.



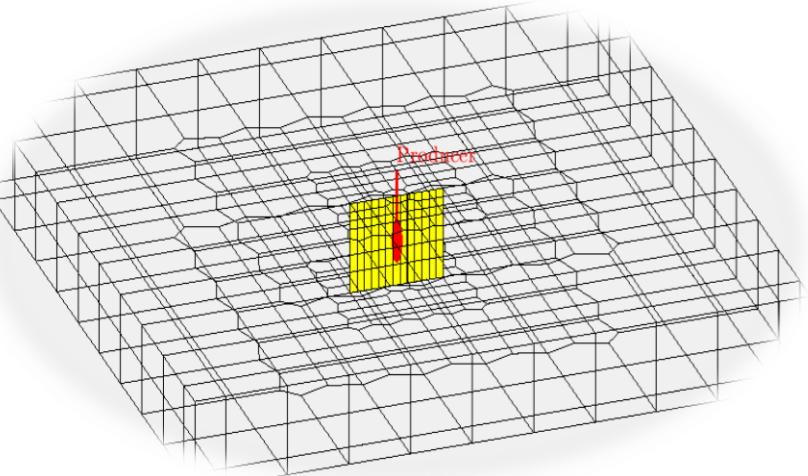
**Sensitivity over Injection Radius to Give Minimum Error:**

- 1- Analytical Solution,  $r_{inj} = 1799$  ft
- 2- Model,  $r_{inj} = 2400$  ft

# Hybrid Grid, Single Well + Hyd. Frac., 1 Case Compared to Eclipse Cartesian Grid

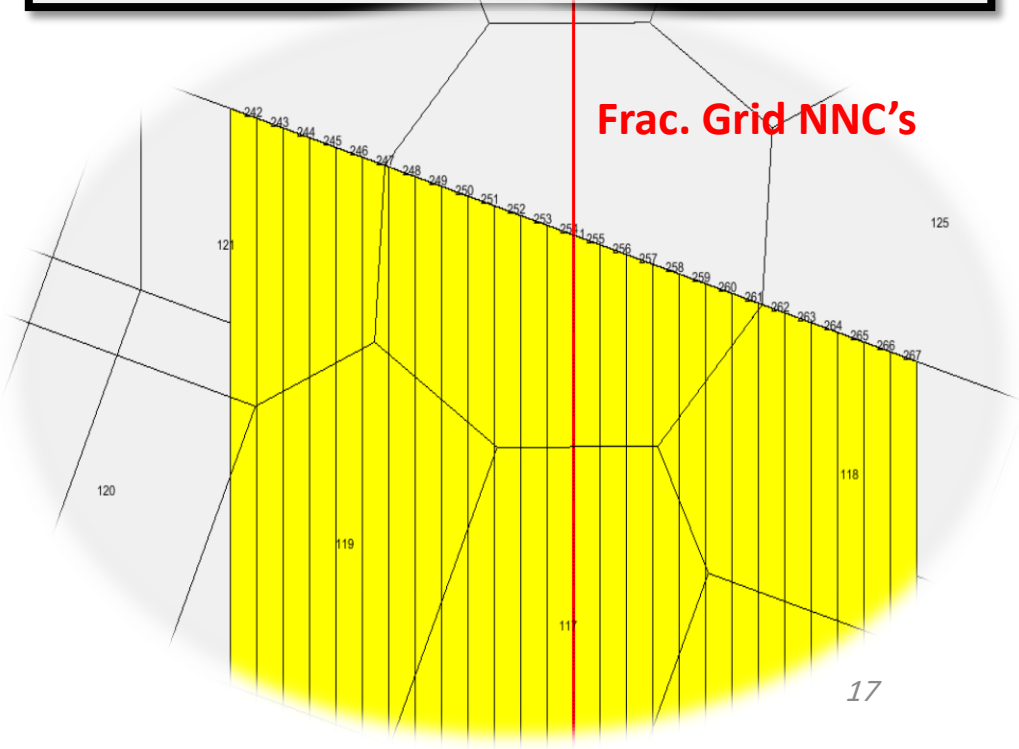
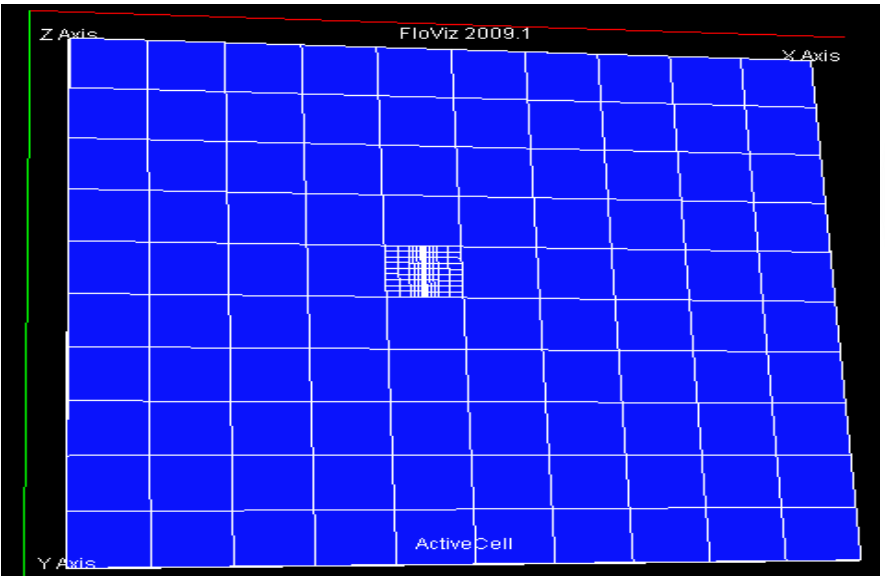
Indexing

Case	Test Type	Phase
8	Draw Down	Gas



231	220	209	183	145	99	61	35	24	13	2					
232	221	210	184	146	100	62	36	25	14	3					
233	222	211	185	147	101	63	37	26	15	4					
234	223	212	187	188	149	150	103	104	65	66	39	40	27	16	5
235	224	213	186	189	148	151	102	105	64	67	38	41	28	17	6
236	225	214	191	192	153	154	110	111	72	73	43	44	29	18	7
237	226	215	190	193	152	155	138	139	106	107	68	69	30	19	8
238	227	216	195	196	160	161	164	117	118	119	74	75	31	20	9
239	228	217	194	197	159	166	167	115	120	121	76	77	32	21	10
240	229	218	199	200	170	165	168	116	122	123	78	79	33	22	11
241	230	219	198	201	169	172	173	130	131	132	80	81	34	23	12
			202	204	177	178	139	140	93	94	55	56			
			203	205	176	179	138	141	92	95	54	57			
			198	201	169	175	128	137	85	91	50	53			
			206	207	181	143	97	59	33	22	11				
			208	182	144	98	60	34	23	12					

## Eclipse Cartesian LGR Grid

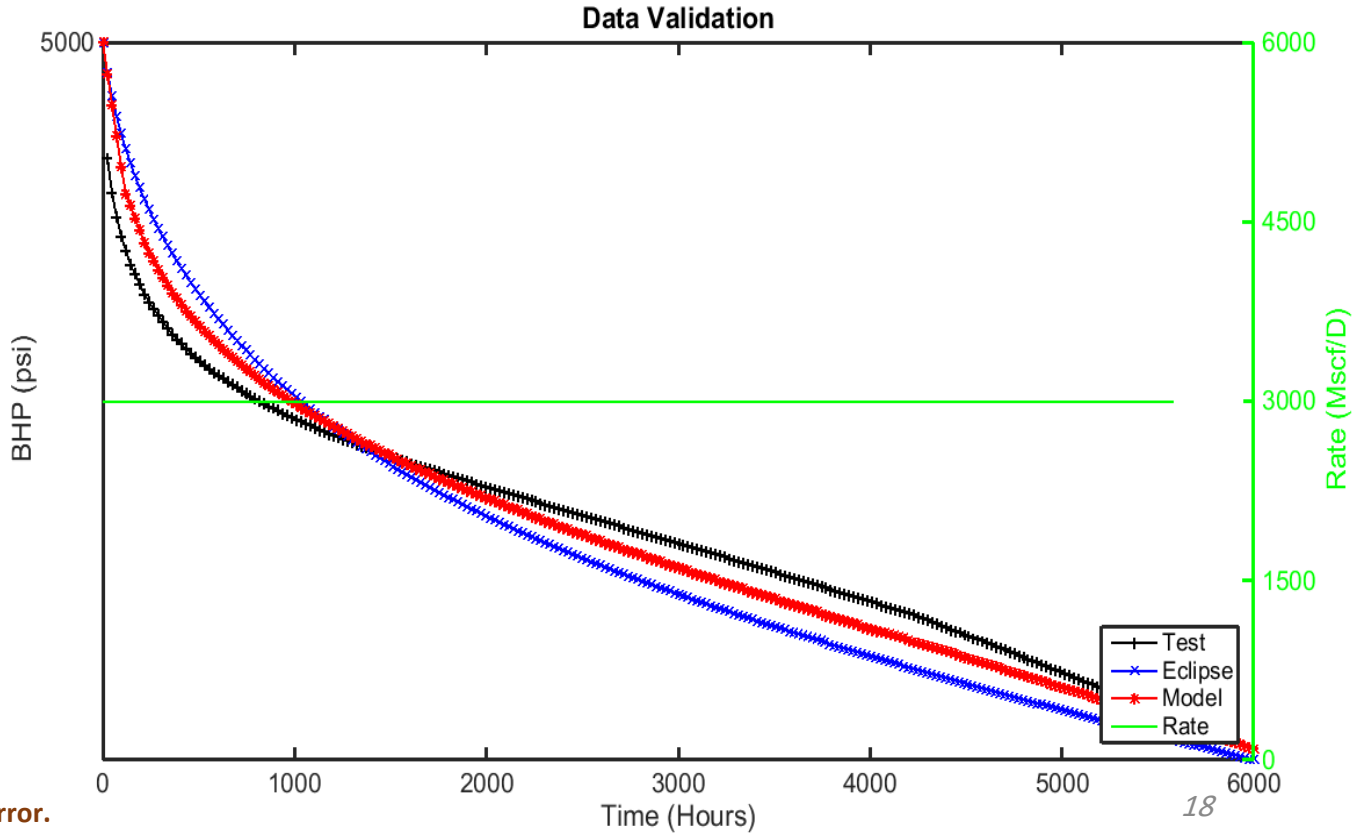


# Case\_8: DD-Gas, 'Fractured Well'

Case_Source	Test Type	Phase	Givens (Model Parameters)
8_ Ex:6.2	Draw Down	Gas	$\gamma_g = 0.65$ , $Q_g = 3,000$ Mscf/D, $h = 60$ ft , $\phi = 0.1$ , $B_g = 0.7085$ RB/ Mscf, $P_i = 5,000$ psia, $C_t = 2.084 \times 10^{-4}$ psi <sup>-1</sup> , $r_w = 0.25$ ft, $z = 0.991$ , $T = 570^\circ\text{R}$ (110°F), and $\mu = 0.01961$ cp

Goodness of Fit Based on NRMSE\*  
Relative to Test Points:

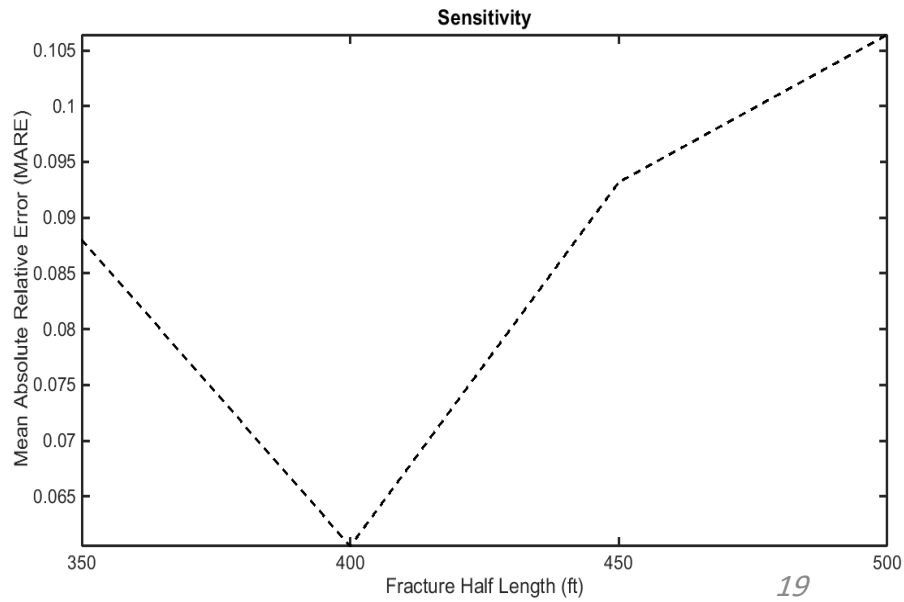
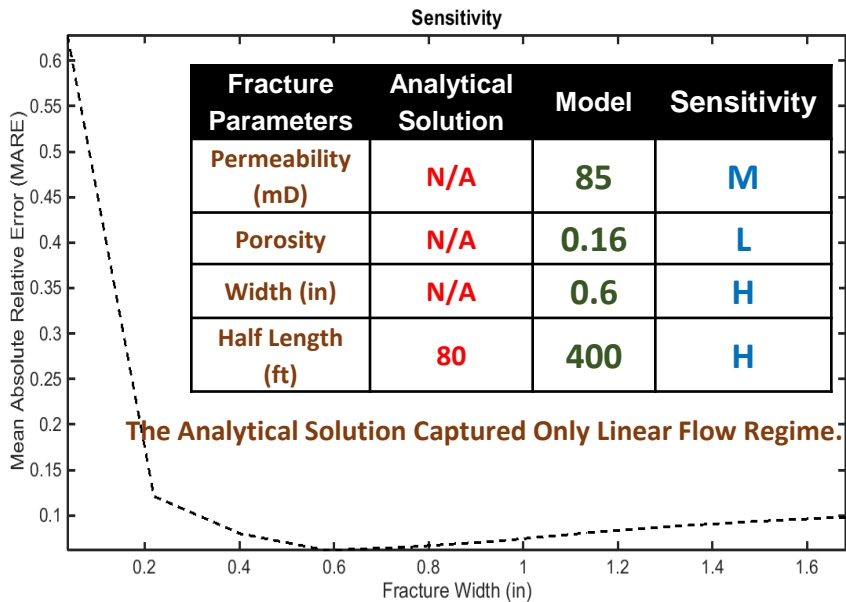
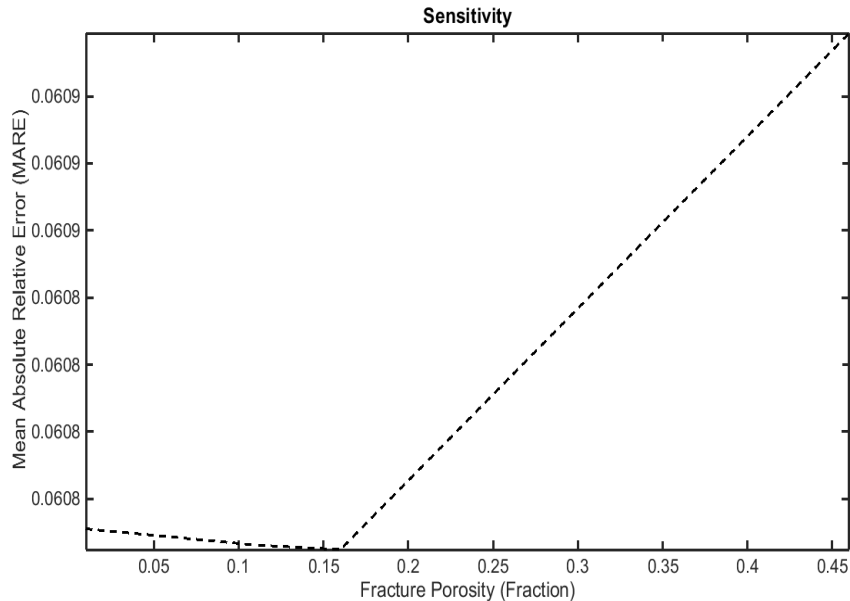
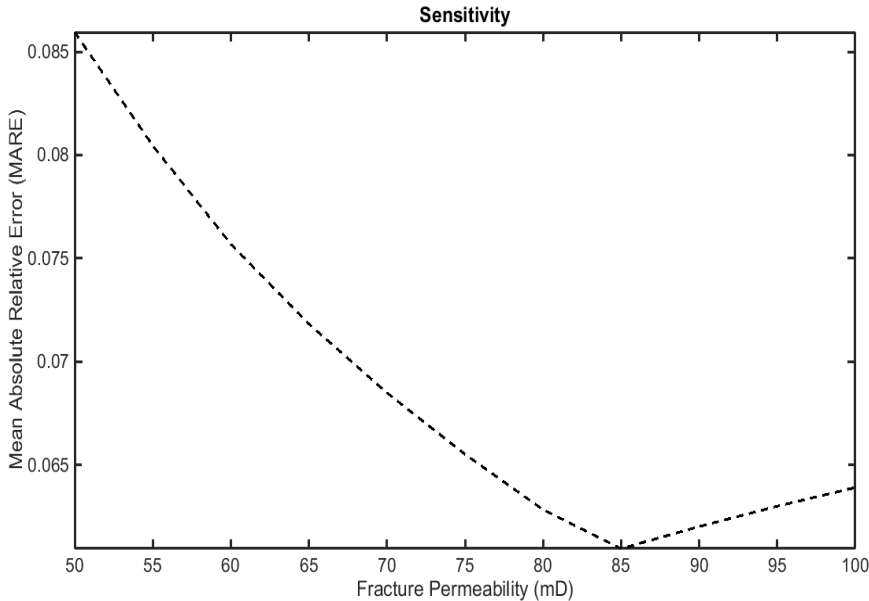
- 1- Eclipse= 0.07
- 2- Model= 0.06



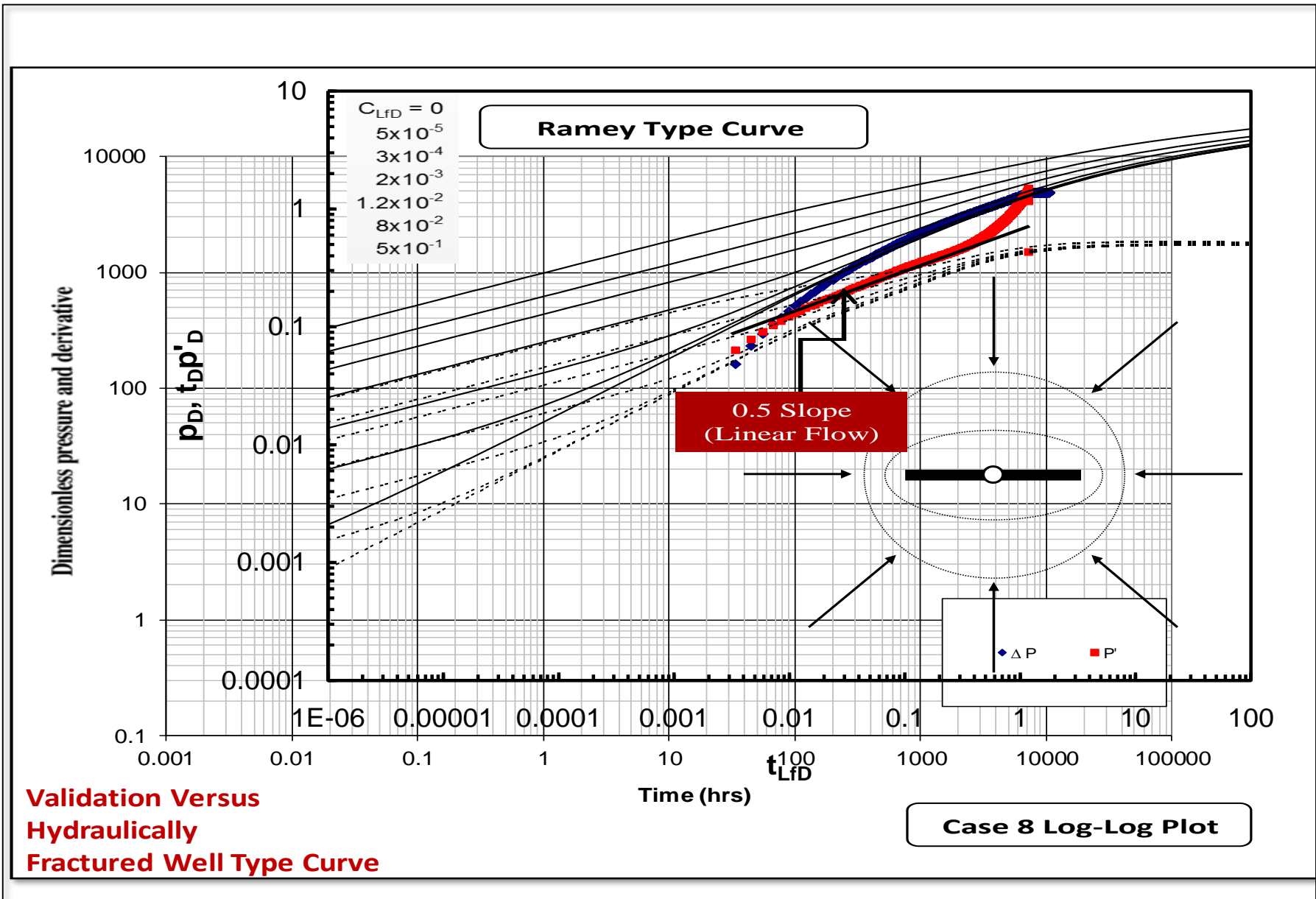
NRMSE\*: Normalized Root Mean Square Error.



# Case\_8: Sensitivities

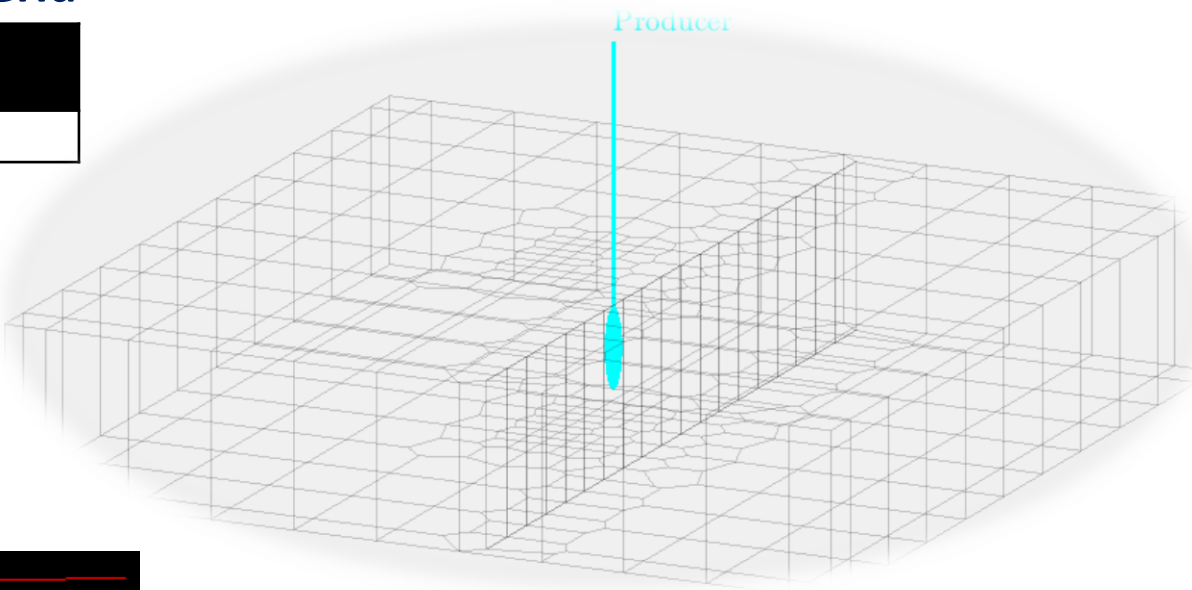


# Case\_8: Validation Versus The Analytical Solution

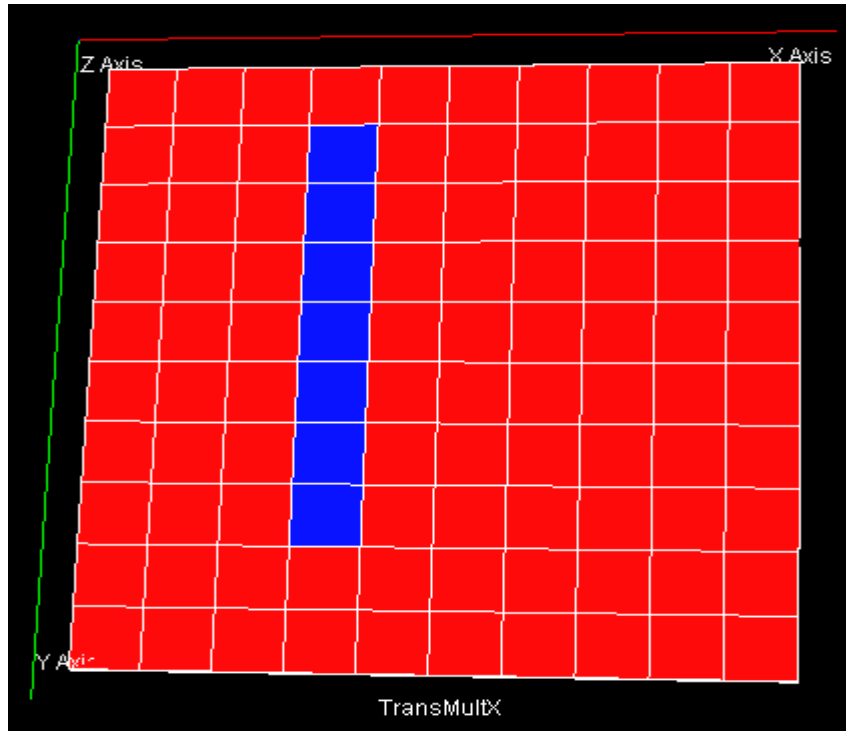


# Hybrid Grid, Single Well, 'Distance to Fault', 1 Case Compared to Eclipse Cartesian Grid

Case	Test Type	Phase
9_Ex:2.11	Build Up	Oil



**Eclipse Cartesian Grid,**  
Representing Fault by Setting  
Transmissibility Multiplier by Zero

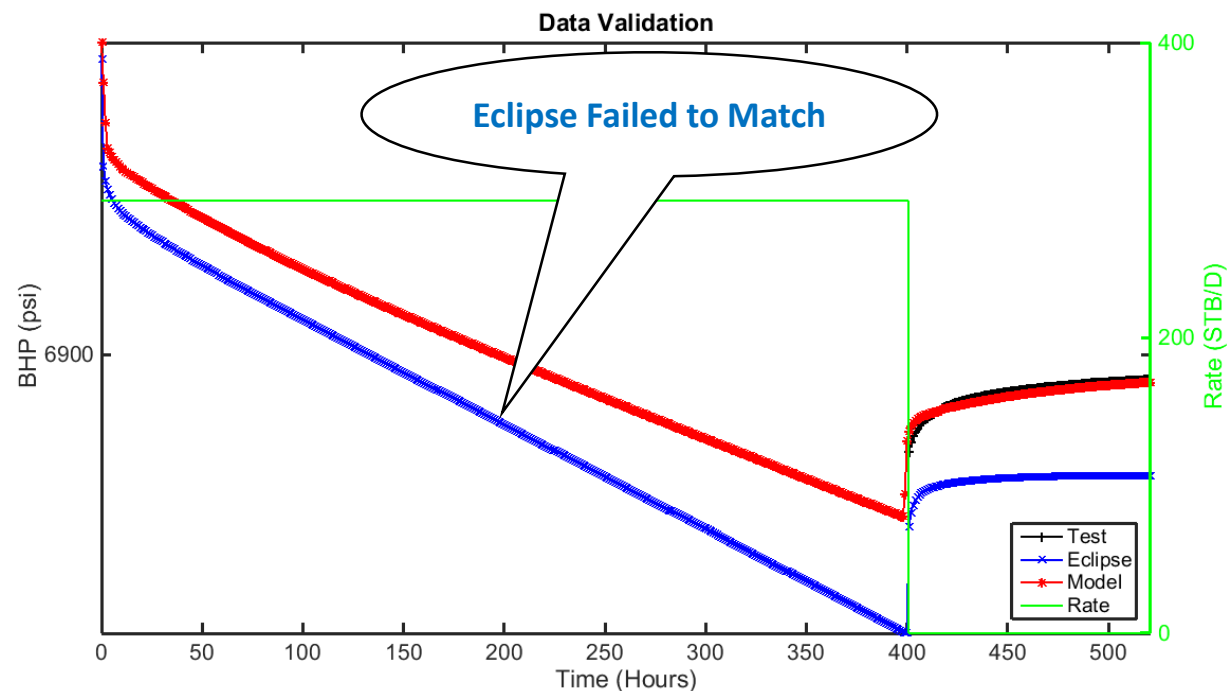


## Indexing

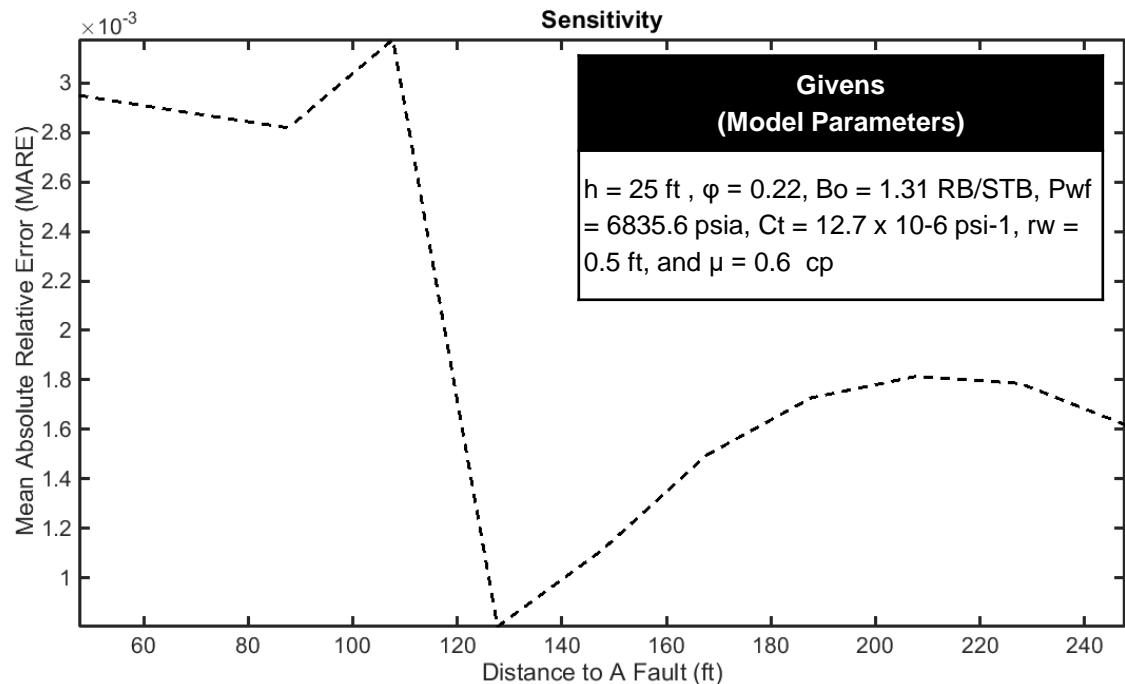
189	178	167	156	124	92	2	84	73	62	51	40
190	179	168	157	125	93	3	21	74	63	52	41
191	180	169	158	126	94	4	22	75	64	53	42
192	181	170	159	127	95	5	23	76	65	54	43
193	182	171	160	128	96	6	24	77	66	55	44
194	183	172	161	129	97	7	25	78	67	56	45
195	184	173	162	130	98	8	26	79	68	57	46
196	185	174	163	131	99	9	27	80	69	58	47
197	186	175	164	132	100	10	28	81	70	59	48
198	187	176	165	133	101	11	29	82	71	60	49
199	188	177	166	134	102	12	30	83	72	61	50

# Case\_9: BU-Oil, 'Distance to Fault'

Goodness of Fit Based on NRMSE\*  
 Relative to Test Points:  
 1- Eclipse= **0.2**  
 2- Model= **0.008** ↓



NRMSE\*: Normalized Root Mean Square Error.

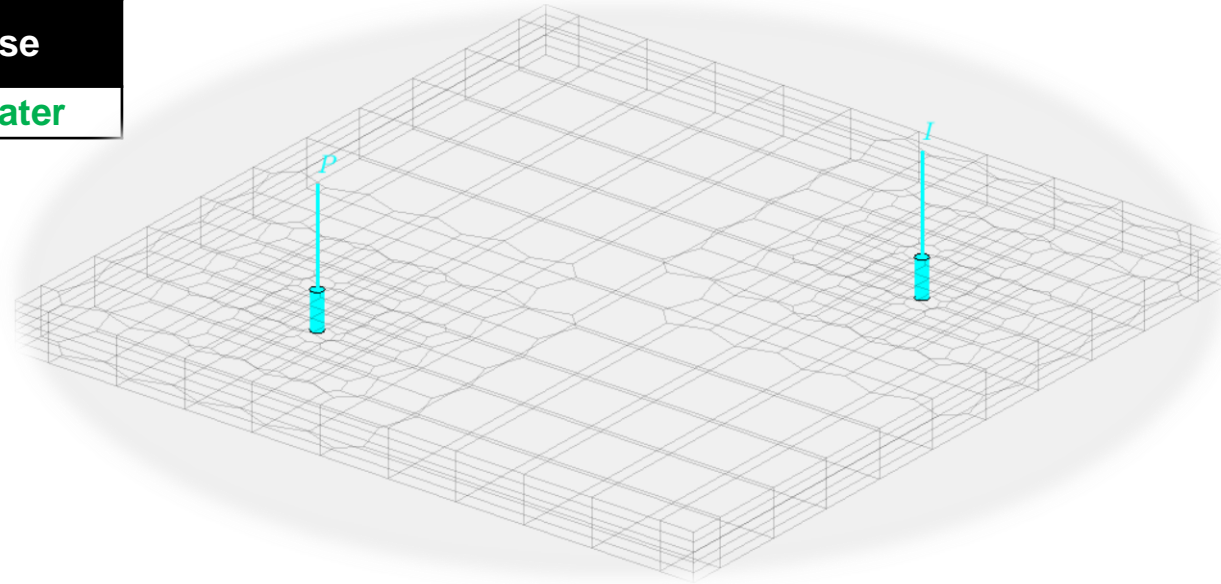


**Sensitivity over Distance to Fault to Give Minimum Error:**

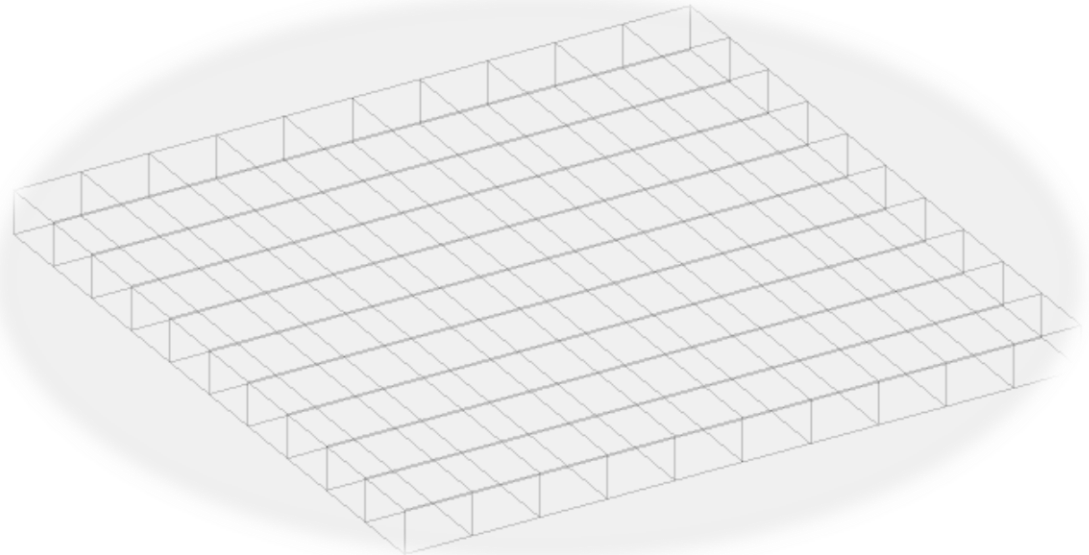
- 1- Analytical Solution,  $x = 147 \text{ ft}$
- 2- Model,  $x = 128 \text{ ft}$

# Hybrid Grid, Two Wells, 'Interference Test', 1 Case Compared to Eclipse Cartesian Grid

Case	Test Type	Phase
10_Ex:10.1	Interference	Oil/Water



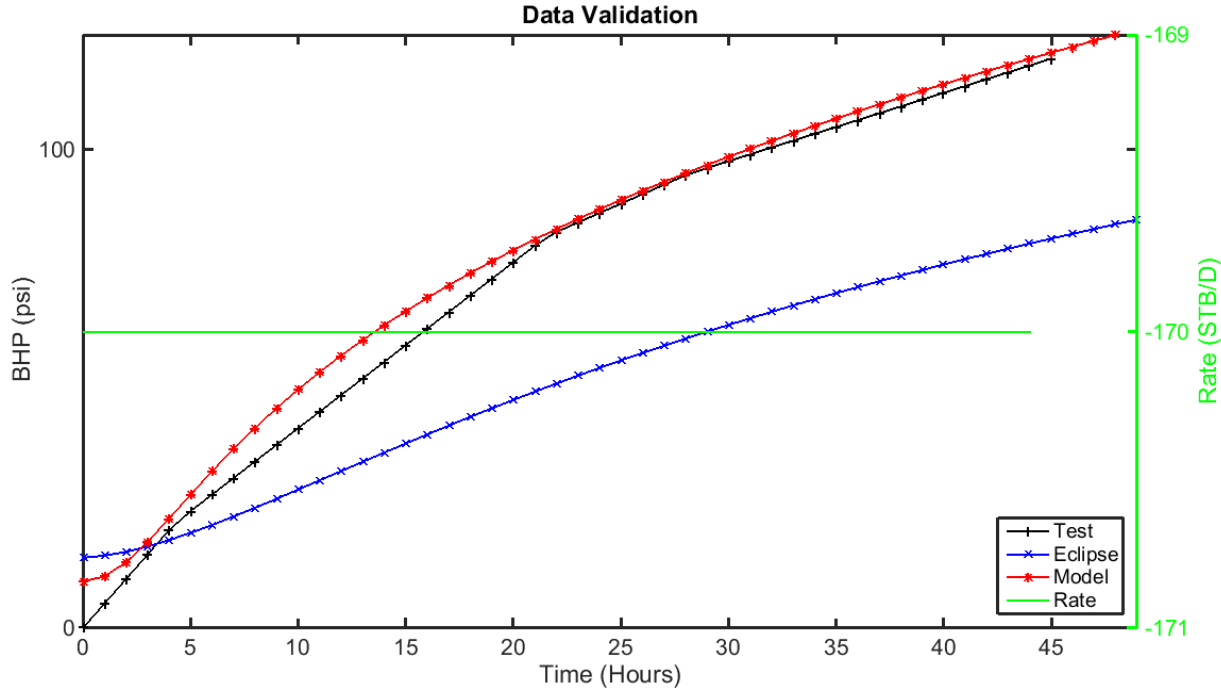
## Eclipse Cartesian Grid,



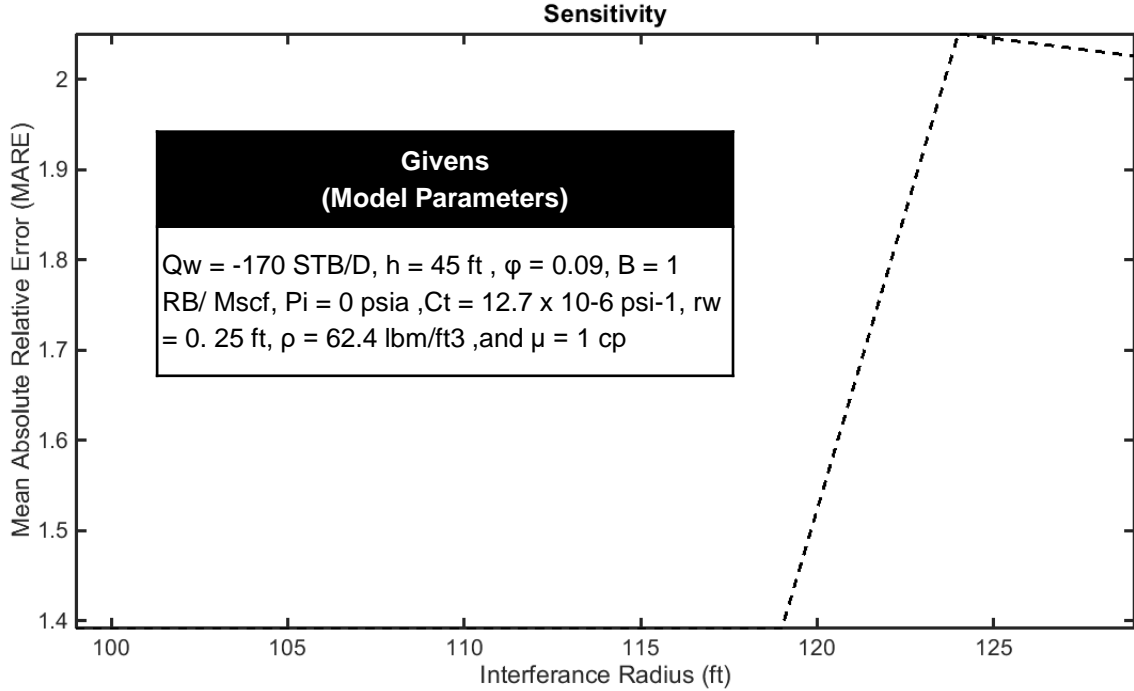
# Case\_10: BU-Oil, 'Distance to Fault'

Goodness of Fit Based on NRMSE\*  
Relative to Test Points:

- 1- Eclipse= 0.8
- 2- Model= 0.2



NRMSE\*: Normalized Root Mean Square Error.

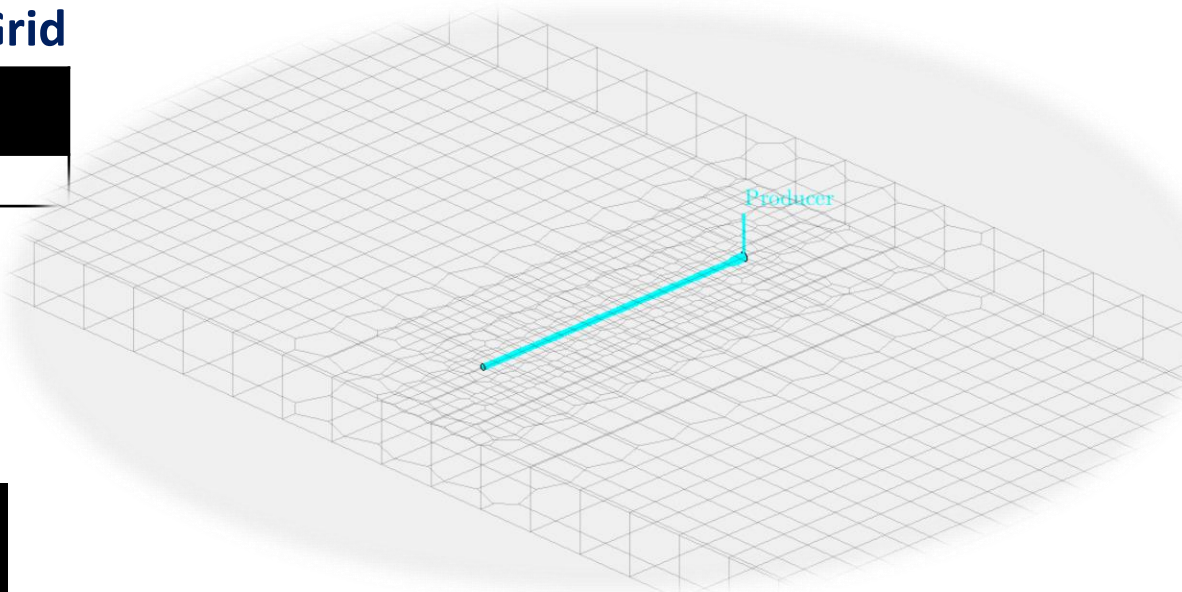


**Sensitivity over Interference Radius to Give Minimum Error:**

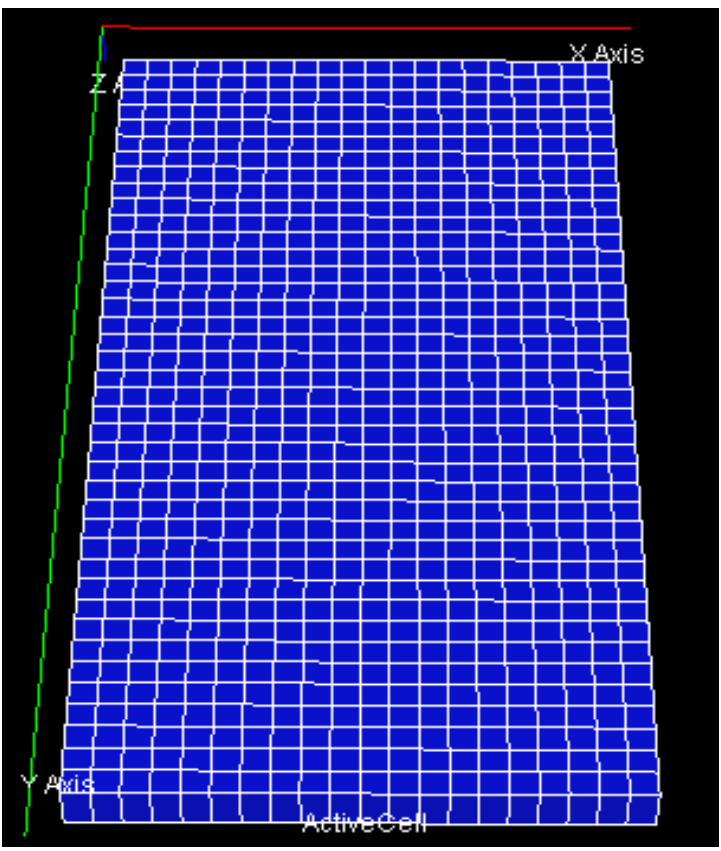
- 1- Analytical Solution, x= 119 ft
- 2- Model, x = 119 ft

# Hybrid Grid, Single Well, 'Hz. Well', 1 Case Compared to Eclipse Cartesian Grid

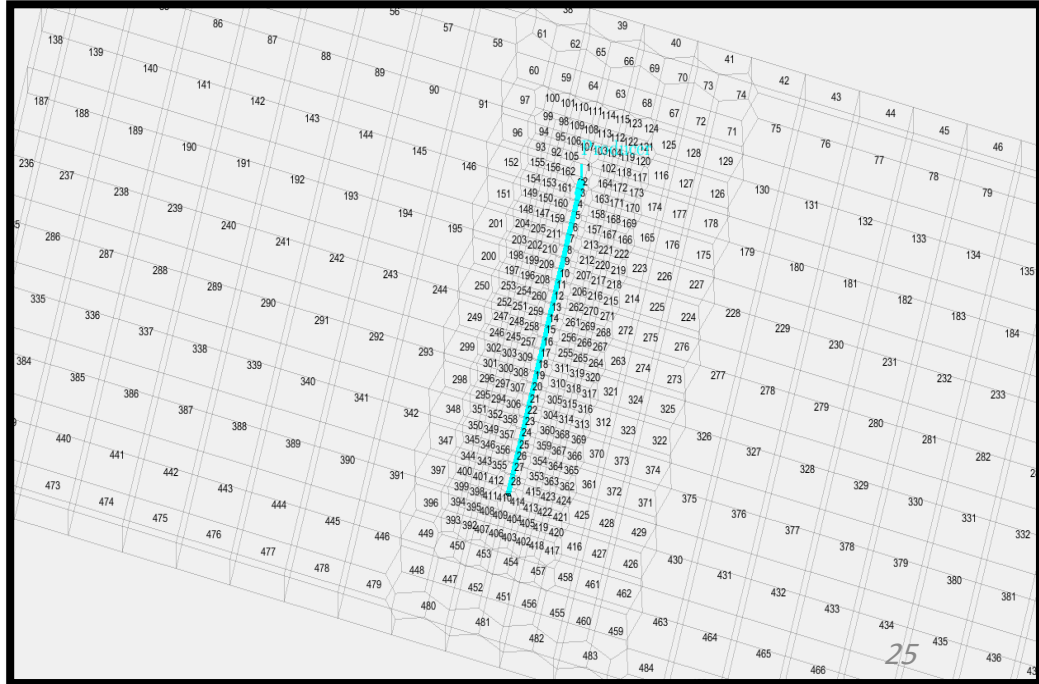
Case	Test Type	Phase
11_Ex:12.1	Draw Down	Oil



## Eclipse Cartesian Grid,



## Indexing



# Case\_11: DD-Oil, 'Hz. Well'

Goodness of Fit Based on NRMSE\*

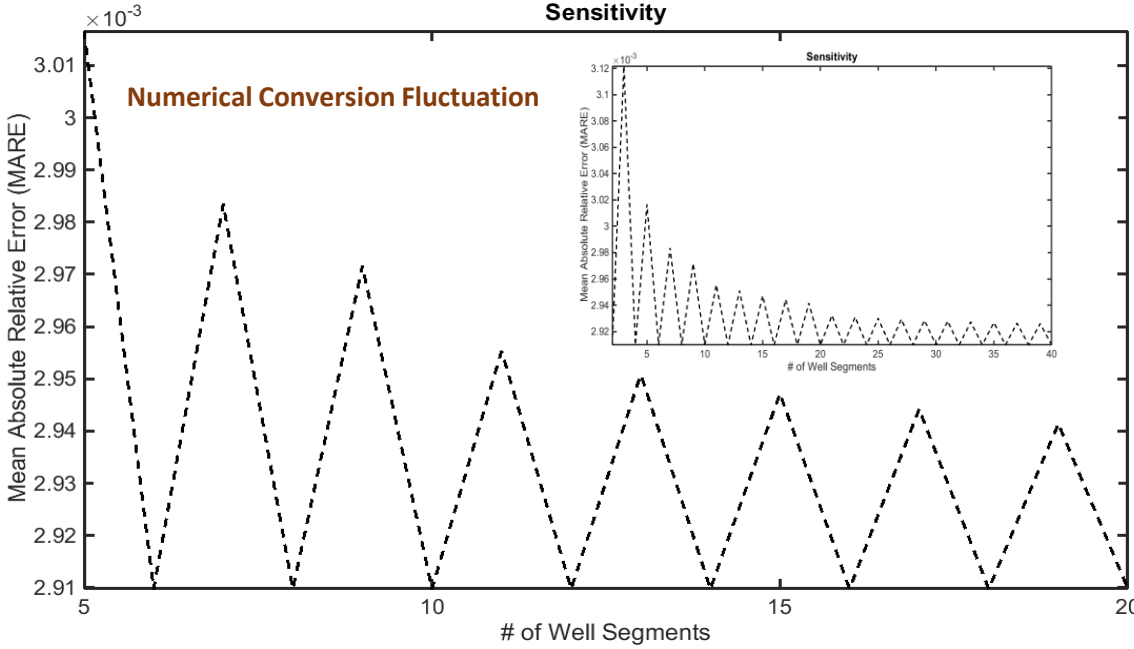
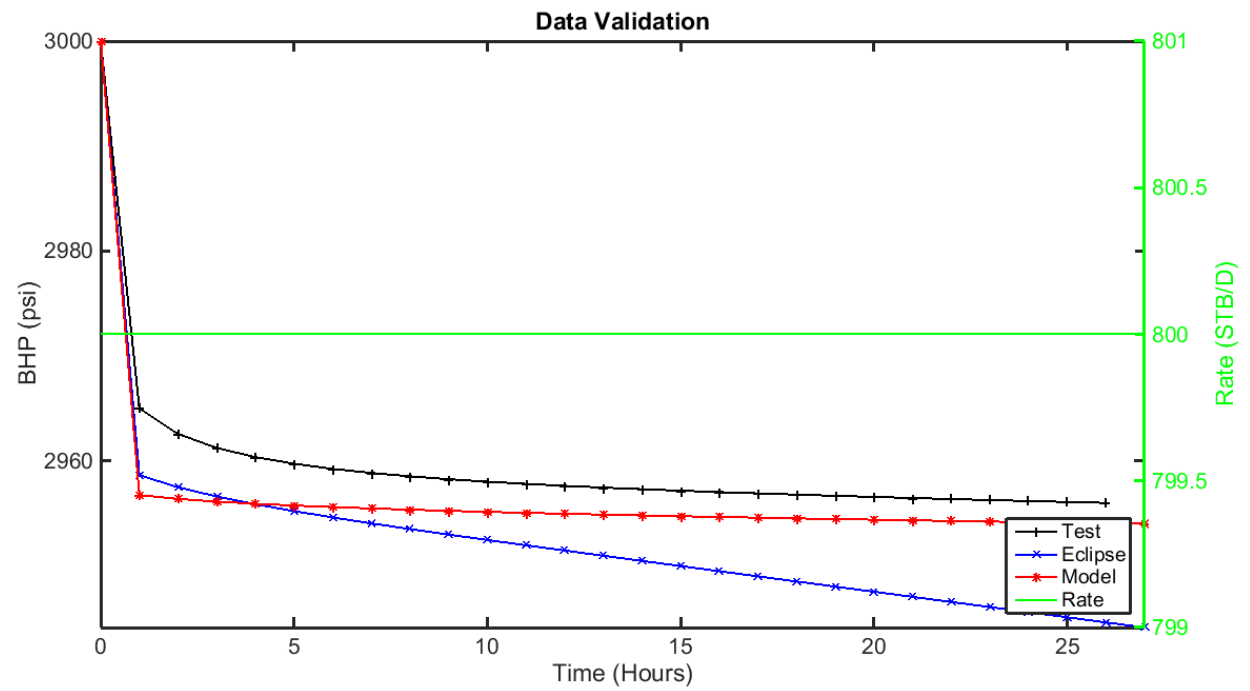
Relative to Test Points:

- 1- Eclipse= **0.0037**
- 2- Model= **0.0029**

**Givens**  
**(Model Parameters)**

$Q_o = 800$  STB/D ,  $h = 200$  ft,  $\phi = 0.2$ ,  $B_o = 1.25$   
 RB/STB,  $P_i = 3000$  psia,  $C_t = 15 \times 10^{-6}$  psi $^{-1}$ ,  $r_w = 0.25$  ft, and  $\mu = 1$  cp  
 Centered in box-shaped drainage area.  
 $h = 200$  ft,  $a = 4,000$  ft, and  $b = 2,000$  ft.  
 $L_w = 1,000$  ft  $k_x = 200$  md

NRMSE\*: Normalized Root Mean Square Error.

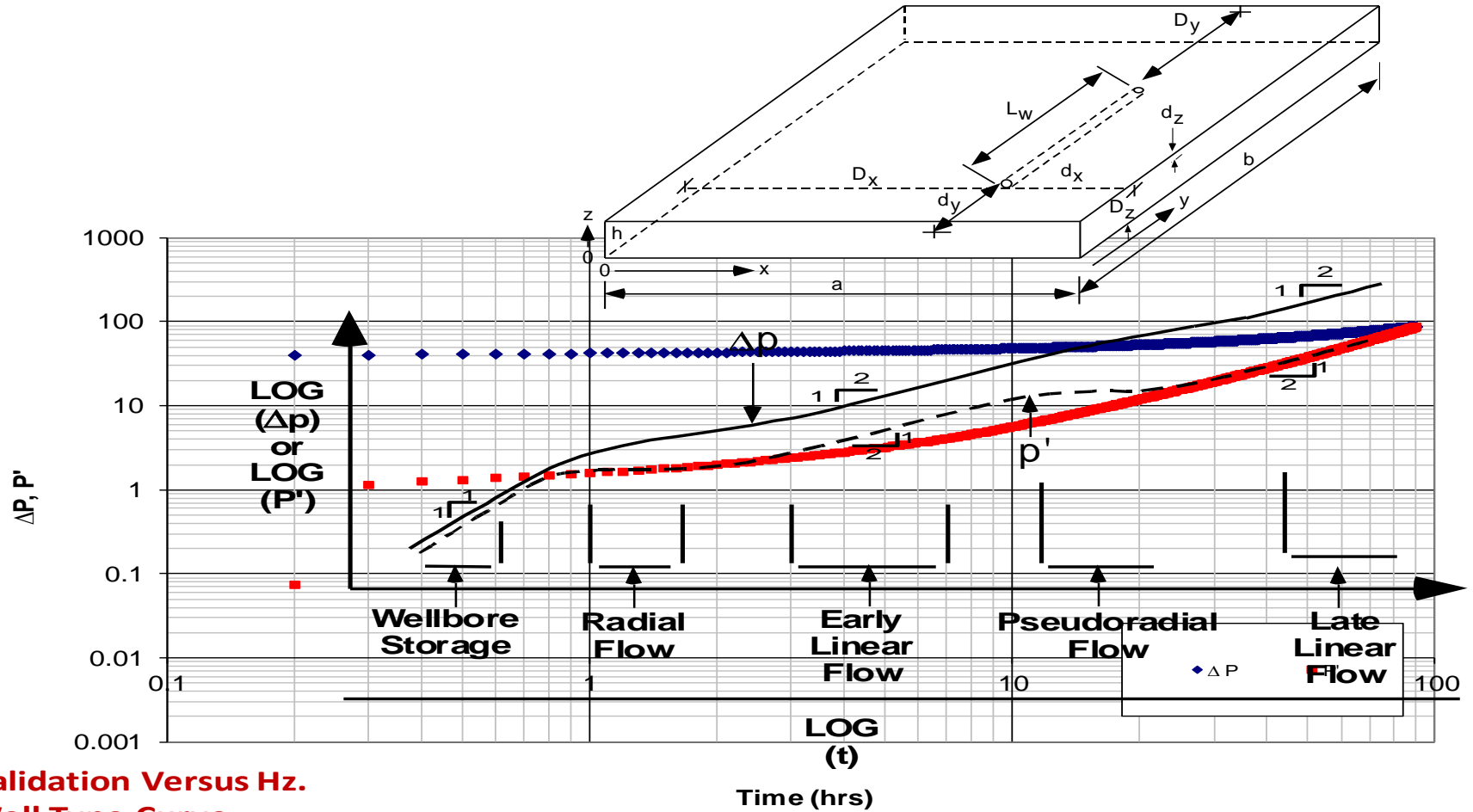


**Sensitivity over # of Well Segments to Give Minimum Error:**

- 1- Analytical Solution, # = **N/A**
- 2- Model , # = **25**



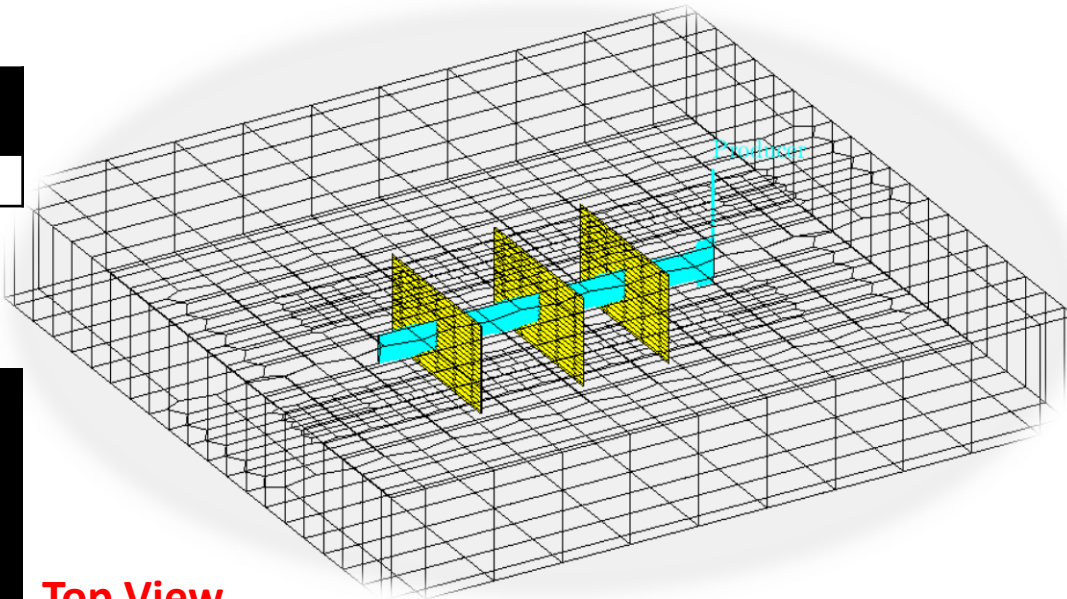
# Case\_11: Validation Versus The Analytical Solution



Validation Versus Hz.  
Well Type Curve

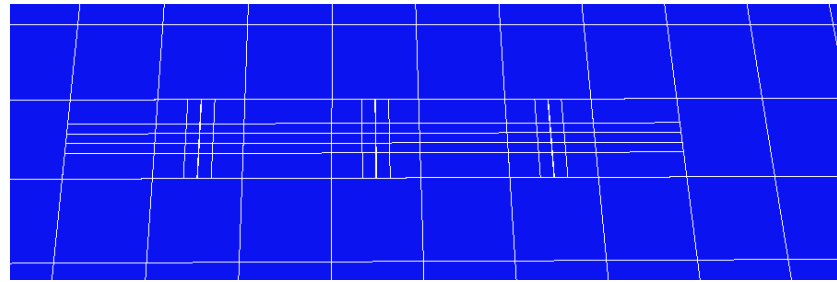
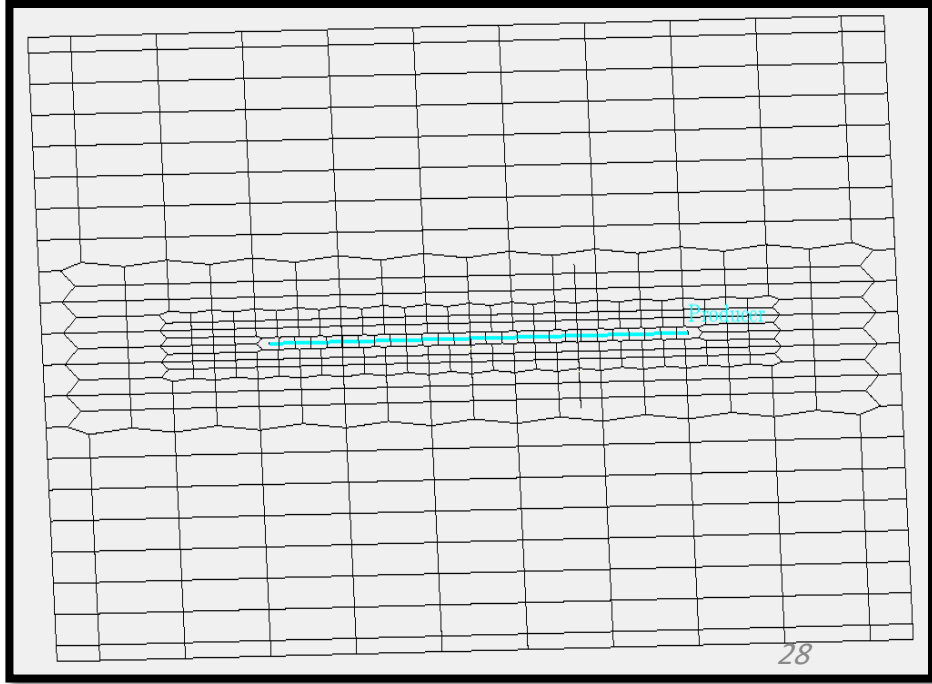
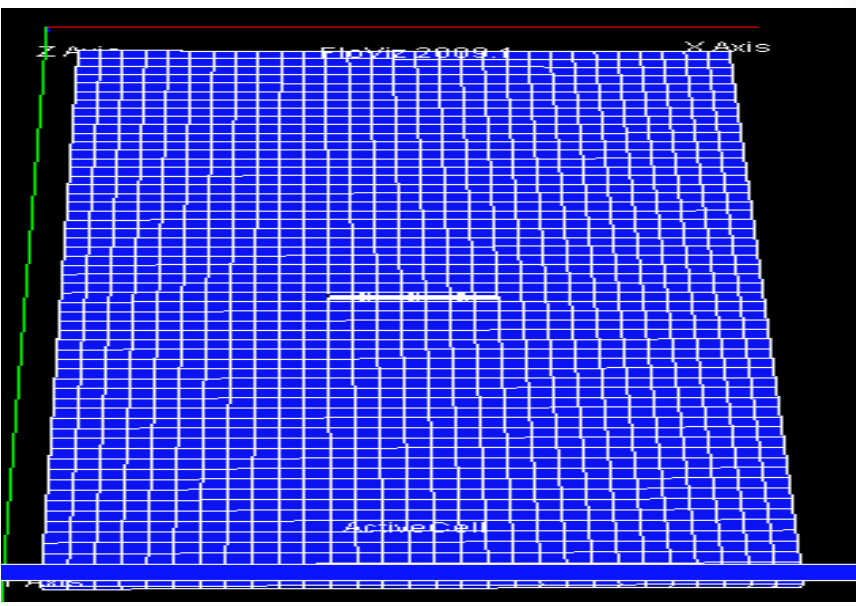
# Hybrid Grid, Single Well , 'Hz. Well + 3 Transverse Fractures', 1 Case Compared to Eclipse Cartesian Grid

Case	Test Type	Phase
12_Hypothetical	Draw Down	Oil



## Eclipse Cartesian LGR Grid,

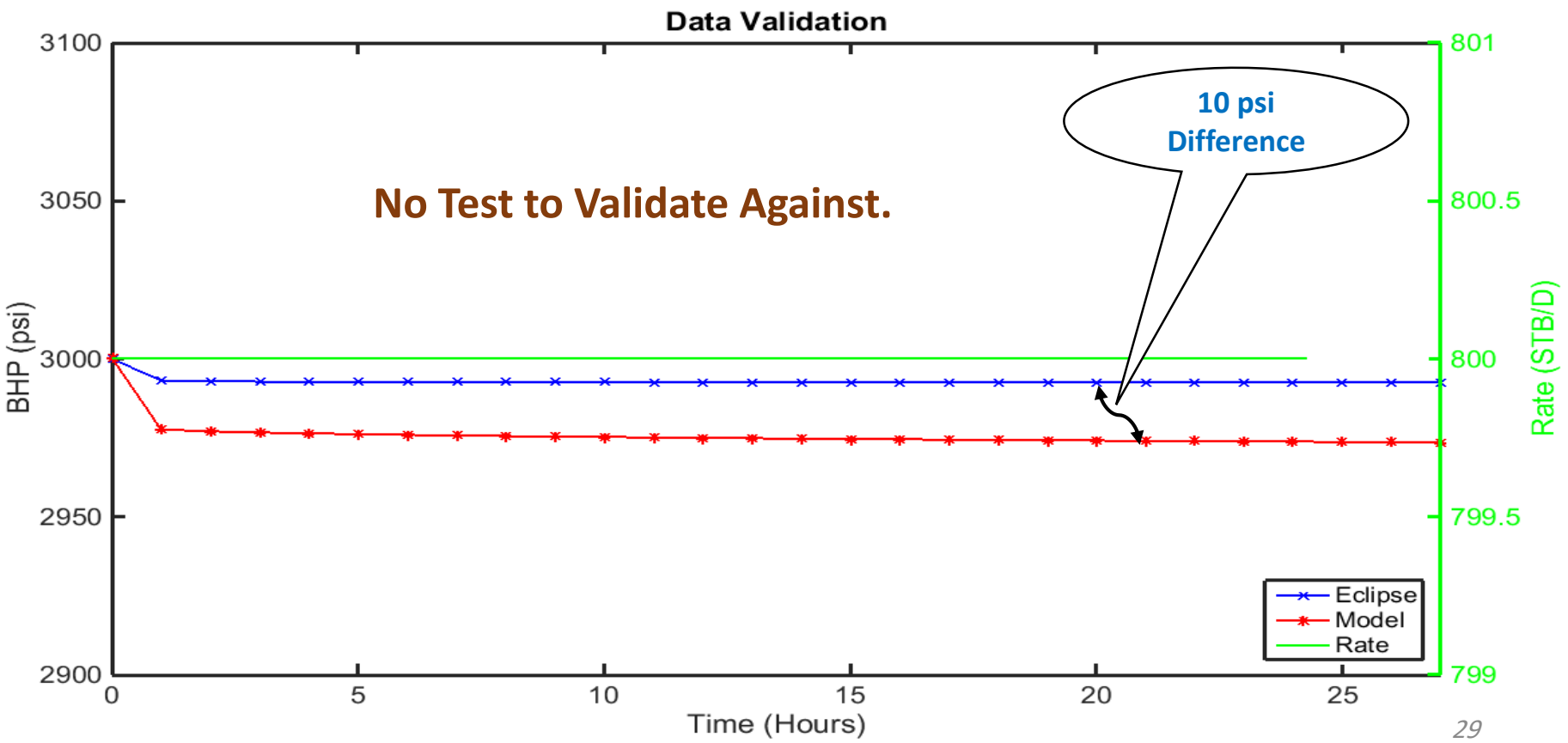
Top View



# Case\_12: DD-Oil, 'Hz. Well + 3 Transverse Fractures'

**Givens  
(Model Parameters)**

$Q_o = 800$  STB/D ,  $h = 200$  ft,  $\phi = 0.2$ ,  $B_o = 1.25$  RB/STB,  $P_i = 3000$  psia,  $C_t = 15 \times 10^{-6}$  psi<sup>-1</sup>,  $r_w = 0.25$  ft, and  $\mu = 1$  cp  
Centered in box-shaped drainage area.  $a = 4,000$  ft, and  $b = 2,000$  ft.  $L_w = 1,000$  ft  $k_x = 200$  md



# Contribution (Added Value): NWT, \*\*SPE 105271/2007



SPE 105271

## Linking Well-Test Interpretations to Full Field Simulations

Faisal M. Al-Thawad, SPE, and Jim S. Liu, SPE, Saudi Aramco, and Raj Banerjee, SPE, and Dominic Agyapong, SPE, Schlumberger

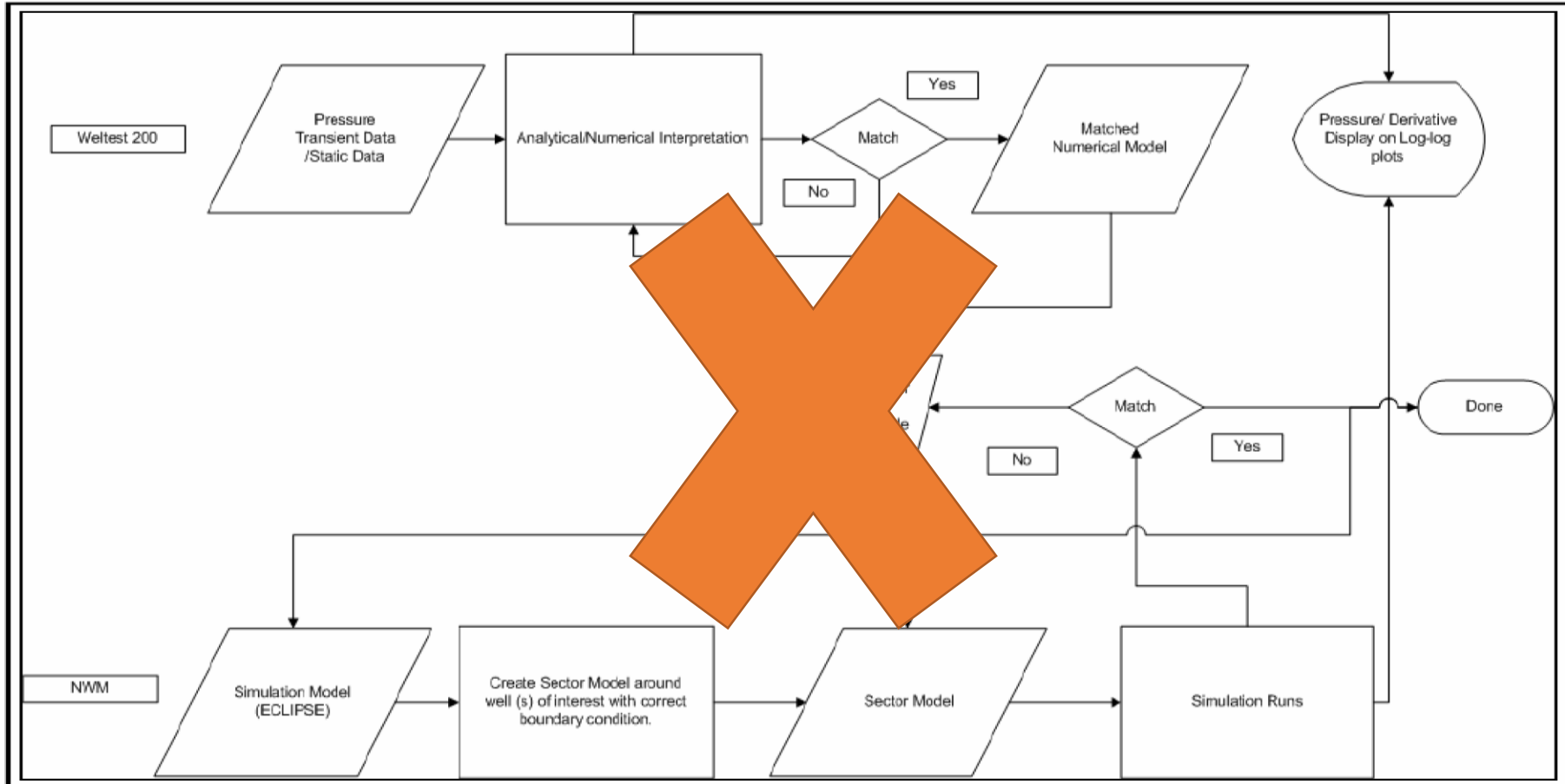


Figure 2: Study Workflow

*Thank You*