## **Polynomial chaos expansions: Exercises**

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## Traveling with constant acceleration

Interactive session: http://10.50.3.247:8888/

Example code: https://github.com/hplgit/chaospy/blob/master/example2.py

Distance when traveling with constant acceleration is

$$s(t) = v_0 t + \frac{1}{2}at^2$$



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Task: Find the expectation value and variance in the time interval t = [0, 10] and plot them. Use:

- Classical Monte Carlo integration.
- Quasi-Monte Carlo using Sobol sequence.
- Pseudo-spectral projection with full tensor grid Gaussian quadrature.
- Pseudo-spectral projection with <u>Clenshaw-Curtis</u> and Smolyak sparse grid.
- Point collocation with random samples and least squares minimization.
- ▶ Point collocation with Hammersley samples and Tikhonov regularization.

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## A Monte Carlo solution gives



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# A different differential equation

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We have the differential equation

$$\frac{du(x)}{dx} = u(x) + a \qquad u(0) = I,$$

where a and I is uncertain and given by

 $a \sim \text{Normal}(4, 1)$   $I \sim \text{Uniform}(2, 6)$ 

Task: Find the expectation value and variance in the time interval t = [0, 1] and plot them. Use:

- ► A pseudo spectral method with a Rosenblat transformation, map against a Normal(0, 1) and Uniform(-1, 1) distribution.
- ► The intrusive Galerkin method.

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## A Monte Carlo solution gives



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