

# Adaptive Multiscale Streamline Simulation and Inversion for High-Resolution Geomodels (SPE 106228)

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## Summary

Objective: direct integration of production data in geomodels

Multiscale-streamline method:

Very fast evaluation of production responses

Generalized travel-time inversion with analytical sensitivities

Selective work reduction based on sensitivities

👉 History matching of million-cell models within the hour!

## Flow Simulator

**Streamline method:**

Mass-conservative streamline formulation [1]

Analytical computation of production sensitivities

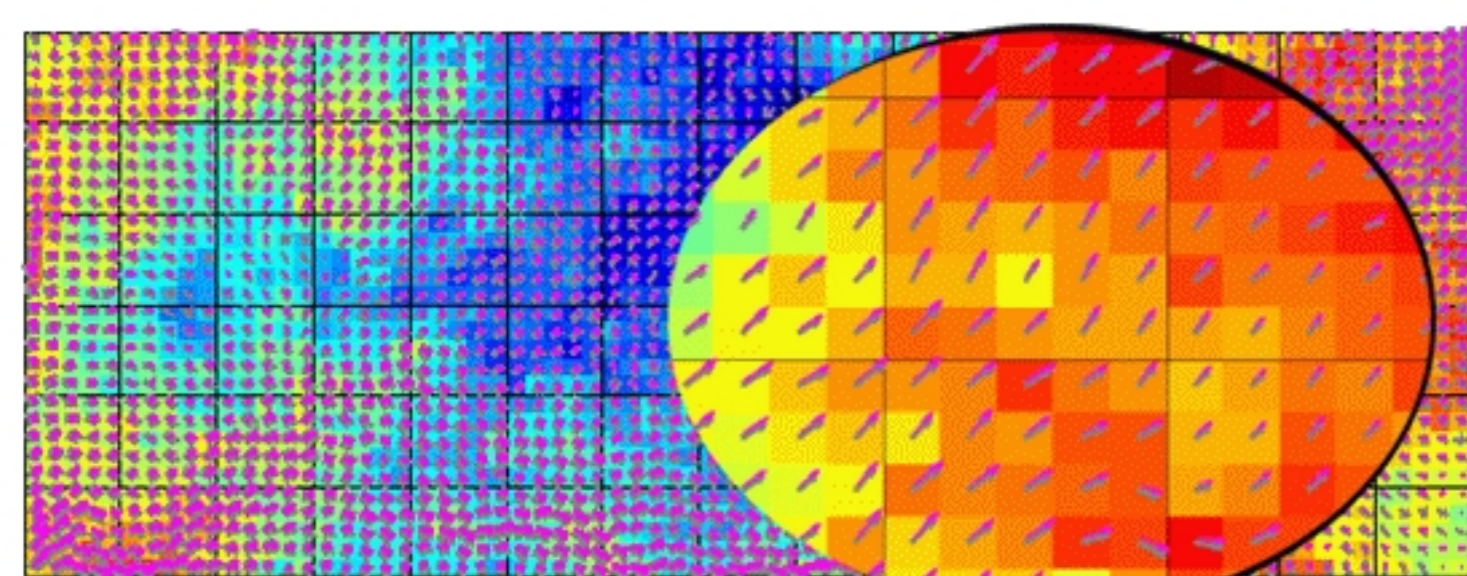
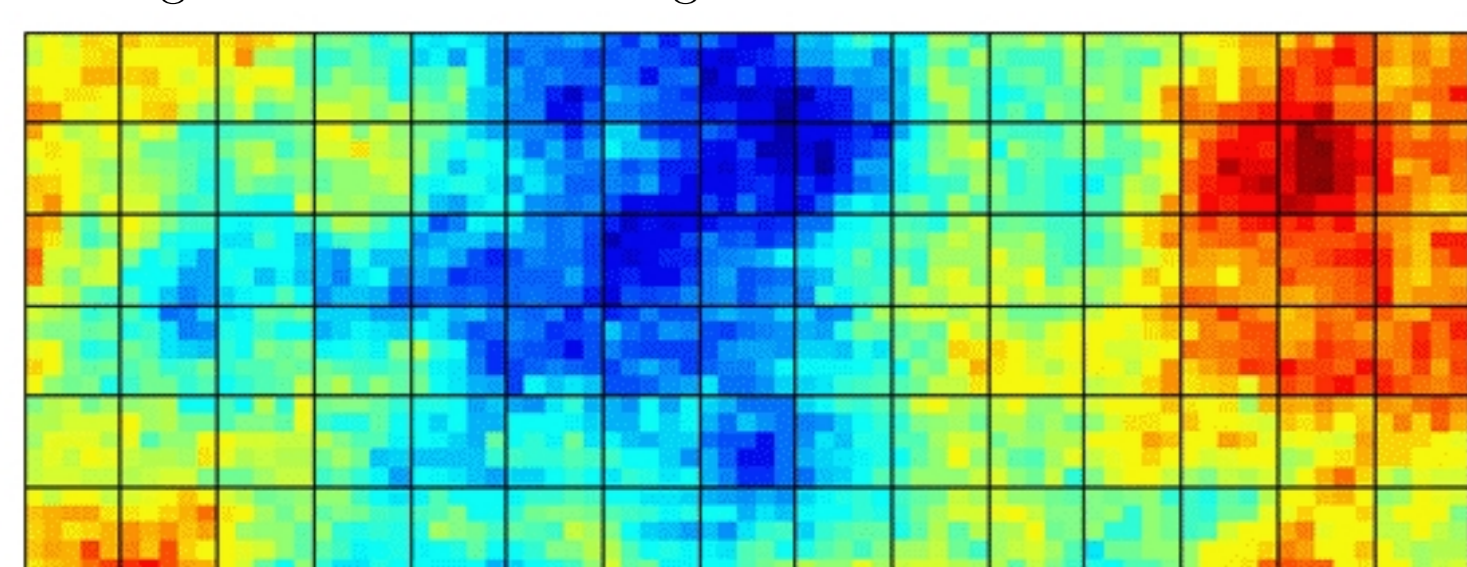
**Multiscale pressure solver (MsMFEM) [2,3]:**

Basis functions: representative *fine-scale* flow patterns inside pairs of coarse blocks. Obtained by solving local flow problems as in flow-based upscaling

Pressure and velocity updated by solving a global problem on the *coarse grid*

Work reduction: basis functions not recomputed in regions that have negligible influence on production responses

Fine grid: 75 × 30. Coarse grid: 15 × 6

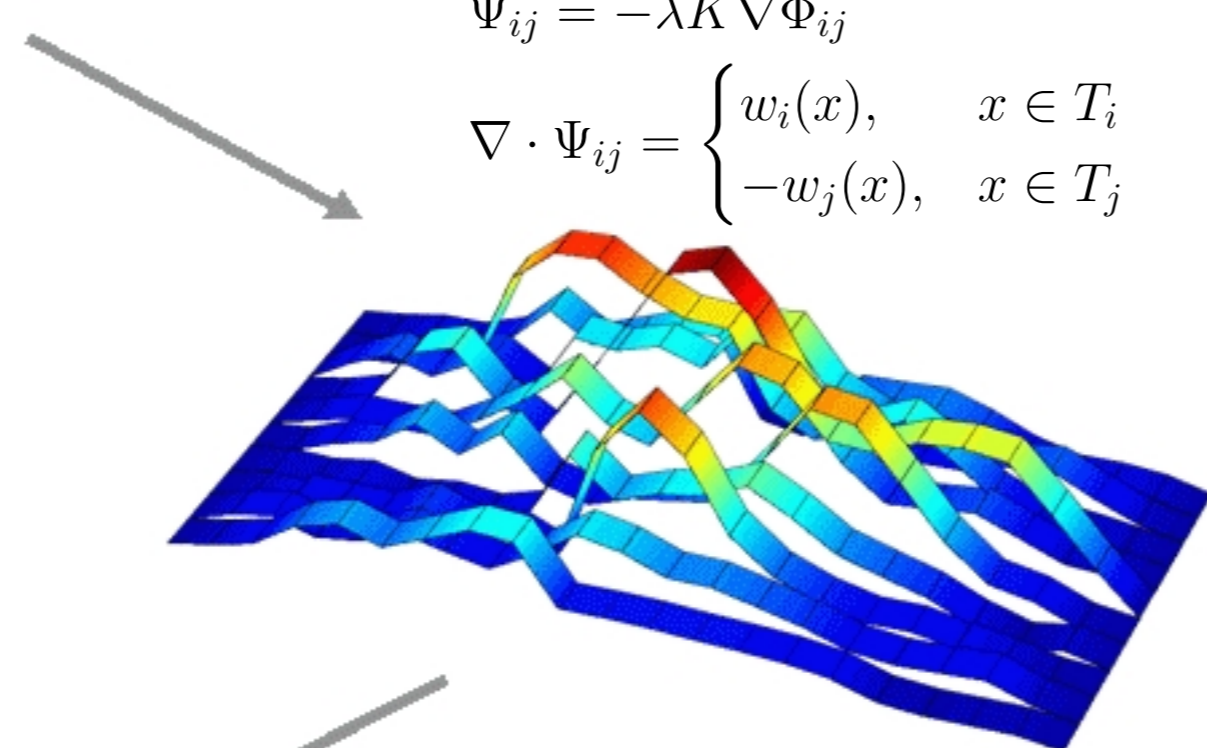


Coarse grid: pressure and fluxes. Fine grid: fluxes

Basis functions for each pair of coarse blocks  $T_i \cup T_j$ :

$$\Psi_{ij} = -\lambda K \nabla \Phi_{ij}$$

$$\nabla \cdot \Psi_{ij} = \begin{cases} w_i(x), & x \in T_i \\ -w_j(x), & x \in T_j \end{cases}$$



Global linear system with 249 unknowns:

$$\nabla \cdot v = q, \quad v = -\lambda K \nabla p$$

Properties of MsMFEM:

- ✓ Incorporates small-scale effects into the coarse-scale solution
- ✓ Mass conservative on coarse grid and subgrid
- ✓ Scalable since basis function are processed independently
- ✓ Flexible: given a fine-grid solver, coarse cell = a collection of connected fine-grid cells
- ✓ Robust: method can always be defined and will always produce a result (in contrast to upscaling)
- ✓ Accuracy: good, provided that coarse grids follow simple guidelines
- ✓ The method is fast when basis functions are update infrequently

## Inversion Method

Generalized travel-time inversion [4,5] minimizes functional:

$$\|\Delta \mathbf{T} - \mathbf{G} \delta \mathbf{k}\| + \underbrace{\beta_1 \|\delta \mathbf{k}\|}_{\text{norm}} + \underbrace{\beta_2 \|\mathbf{L} \delta \mathbf{k}\|}_{\text{smoothing}}$$

Here:  $\Delta \mathbf{T}$  = travel-time shifts,  $\mathbf{G}$  = sensitivity matrix,  $\mathbf{k}$  = permeability

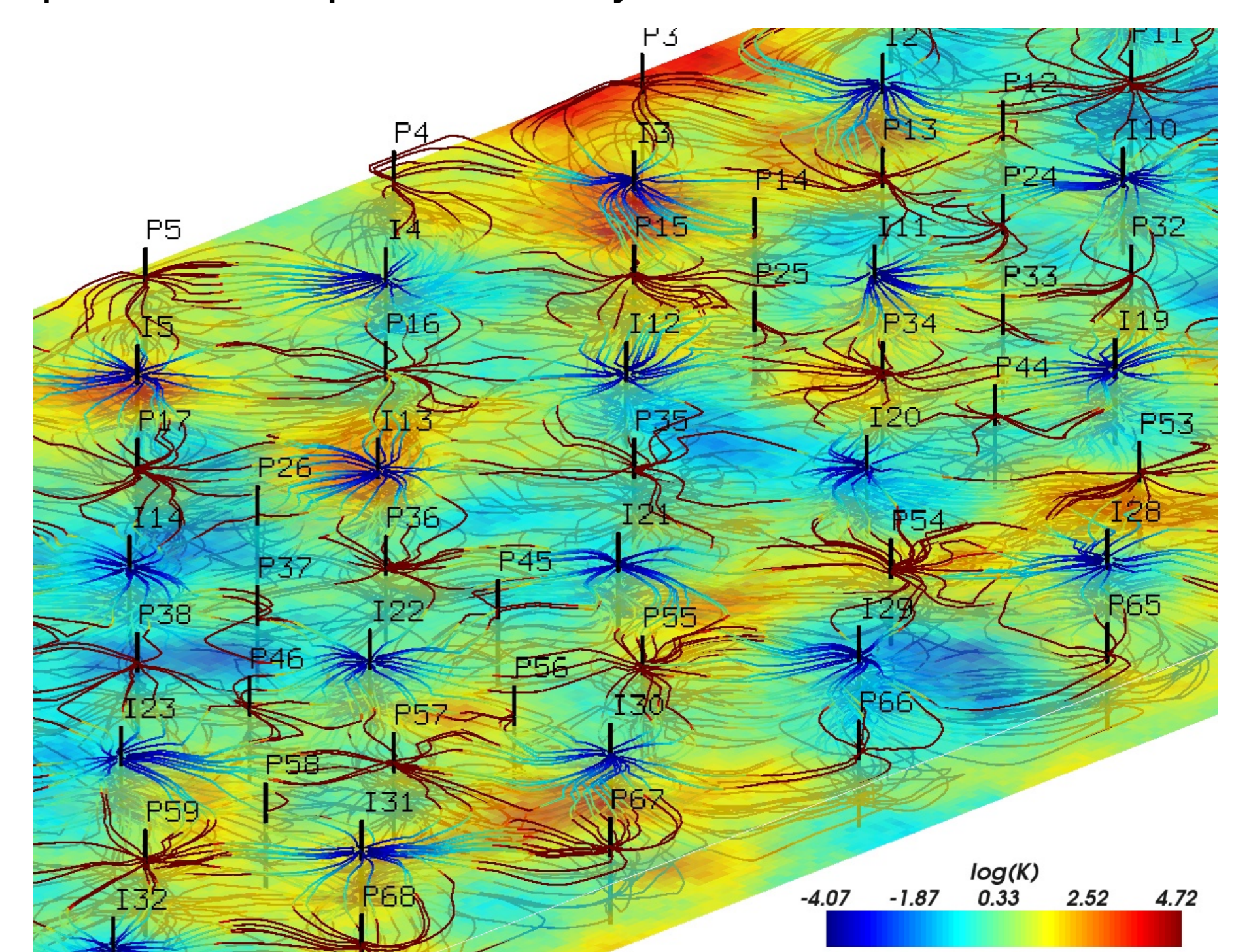
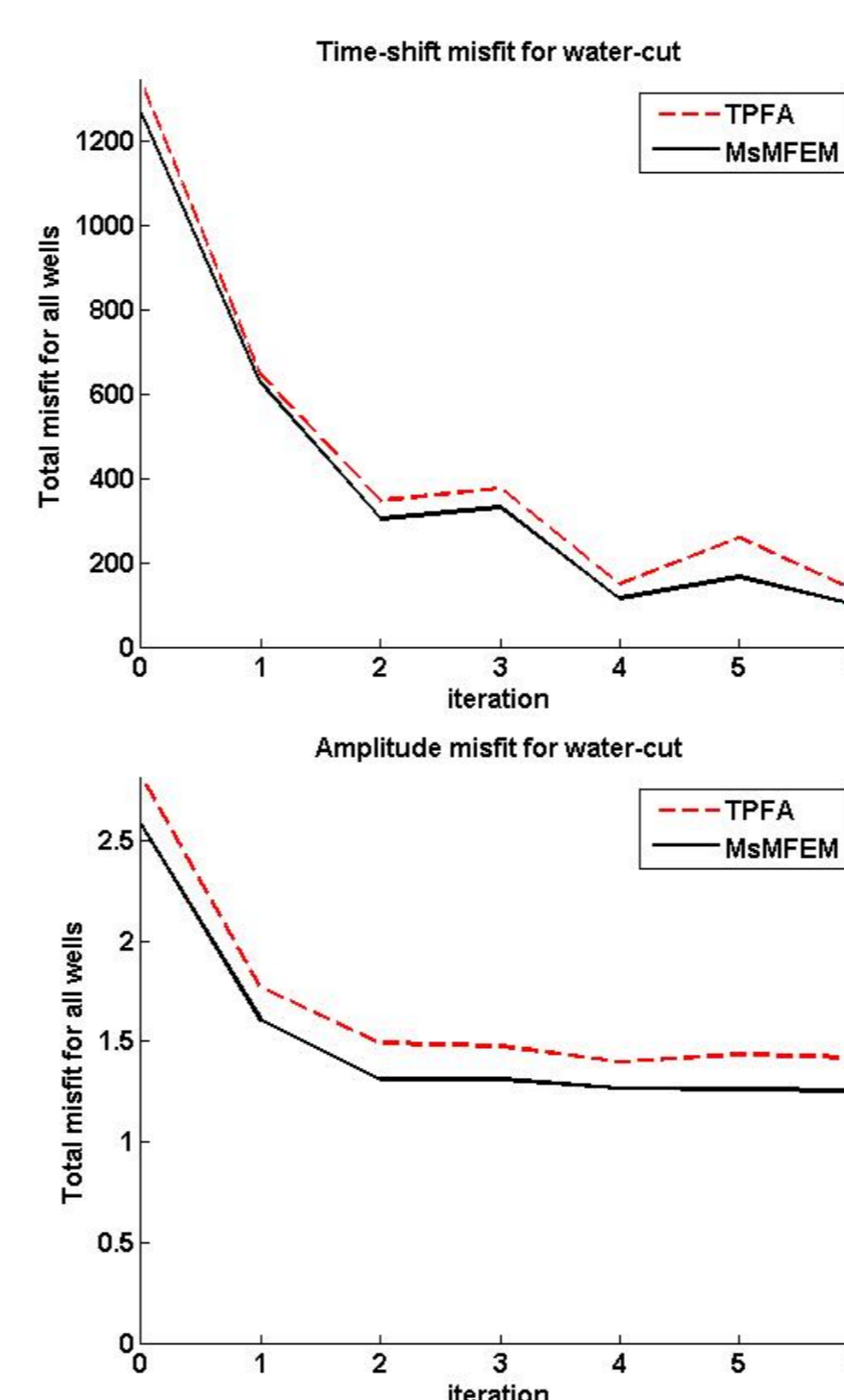
✓ Solution by a least-squares algorithm

✓  $\mathbf{G}$  computed analytically based on a single forward simulation

## Results

History match of a high-resolution 3D geomodel:

- Fine-grid: 256 × 128 × 32 (1,048,576 active cells)
- Coarse-grid: 32 × 16 × 8 (each coarse cell 8 × 4 fine cells)
- 32 injectors and 69 producers (vertical wells)
- Incorporating 2475 days of water-cut data (almost 7 years) to adjust permeability
- Each forward simulation: 15 pressure steps of 165 days



Pressure solver	Reduction in % for misfit		$\overline{\Delta \log k}$	CPU time 2.4 GHz
	Time-shift	Amplitude		
Initially	100.0	100.0	0.821	—
7-point FV (TPFA)	9.6	50.4	0.806	39min
MsMFEM	7.6	48.7	0.808	17min

## Conclusions

The new multiscale-streamline method:

- ✓ allows rapid history matching of large reservoir models
- ✓ matched 7 years of production history in 17 minutes for a million-cell reservoir model with 69 producers
- ✓ gave significant reductions in computational time using selective updating of basis functions
- ✓ gives updated models that are geologically realistic
- ✓ applies in principle to more complicated grids (corner-point, unstructured)

## References

- [1] V. Kippe, H. Hægland, and K.-A. Lie. A method to improve the mass balance in streamline methods. SPE 106250, SPE 07 RSS, Houston, 26–28 February, 2007.
- [2] Z. Chen and T.Y. Hou. A mixed multiscale finite element method for elliptic problems with oscillating coefficients. *Math. Comp.*, 72:541–576, 2003.
- [3] J.E. Aarnes, V. Kippe, and K.-A. Lie. Mixed multiscale finite elements and streamline methods for reservoir simulation of large geomodels. *Adv. Water Resour.*, 28(3):257–271, 2005.
- [4] D.W. Vasco, S. Yoon, and A. Datta–Gupta. Integrating dynamic data into high-resolution reservoir models using streamline-based analytic sensitivity coefficients. *SPE J.*, pp. 389–399, December 1999.
- [5] Z. He, S. Yoon, and A. Datta–Gupta. Streamline-based production data integration with gravity and changing field conditions. *SPE J.*, pp. 423–436, December 2002.

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